

# Medical image registration

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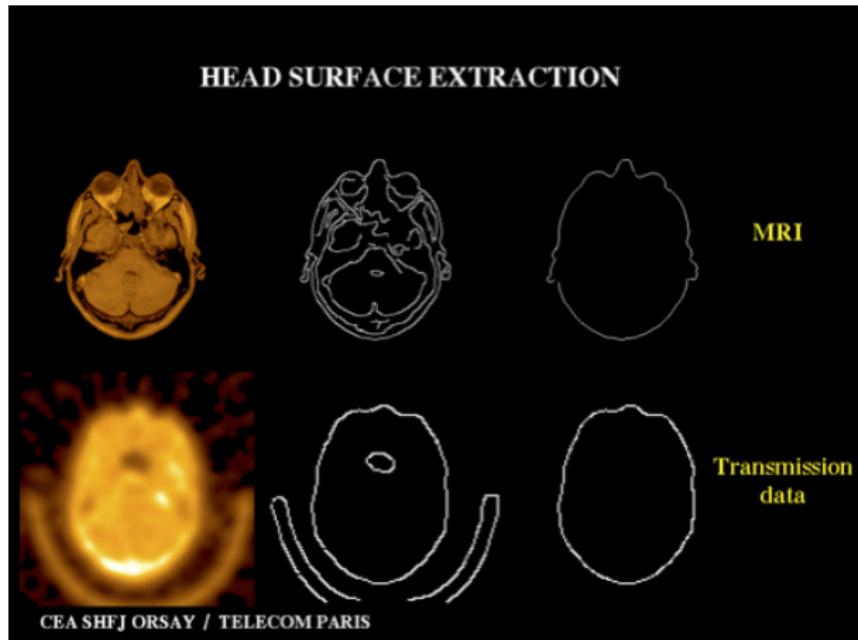
[isabelle.bloch@sorbonne-universite.fr](mailto:isabelle.bloch@sorbonne-universite.fr)

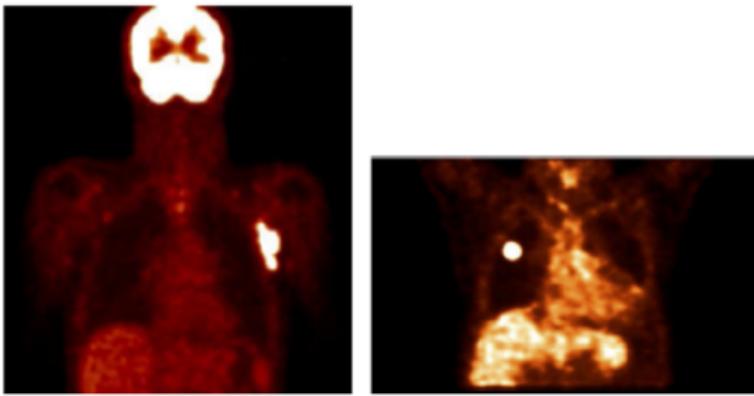
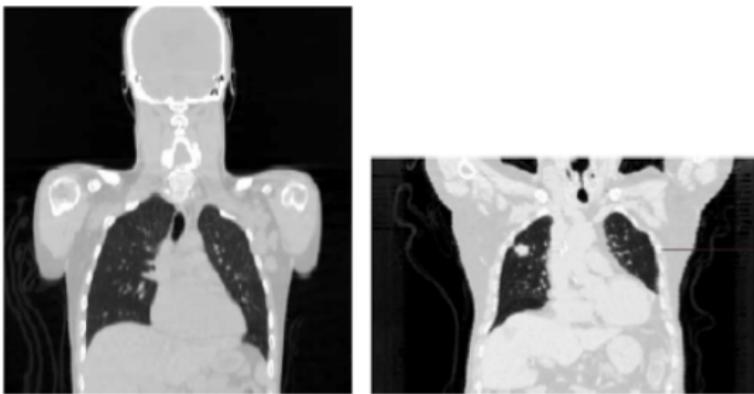


# Introduction

- Usefulness of registration
- Multi-modal imaging
- Complementary information
- Preprocessing for fusion
- More information and better decisions

# Why and How?





# Definition

## Finding the best spatial correspondence

General formulation:

$$\min_{t \in \mathcal{T}} f(I_1, t(I_2))$$

- $I_1$  and  $I_2$ : images to register (or features extracted from the images)
- $t$ : transformation
- $\mathcal{T}$ : set of possible / admissible transformations
- $f$ : distance (or similarity  $\Rightarrow \max f$ )

# Main components of a registration system

- nature of the transformation ( $t$  and its domain  $\mathcal{T}$ )
- features (on which  $t$  and  $f$  are applied)
- distance or similarity criterion  $f$
- optimization method

non mutually independent  
depend on the type of images, modalities,  
and on the registration problem to solve

## Difficulties due to

- complexity of problems
- discrete nature of images
- evaluation of registration results

# Types of problems

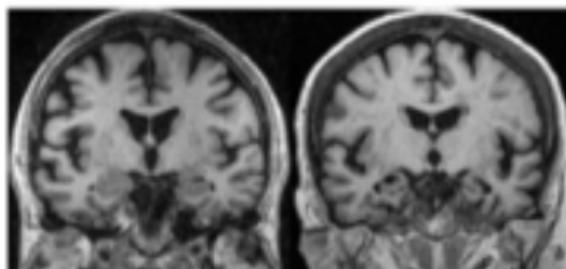
- 2D/2D, 2D/3D, 3D/3D
- mono-modal images
- multi-modal images
- image / model (e.g. anatomical atlas)
- inter-patient registration

# Example

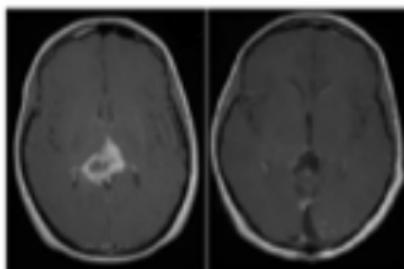


Same modality  
Different subjects

Different modalities  
Same subject



Longitudinal study



Pre and postoperative

# Transformations

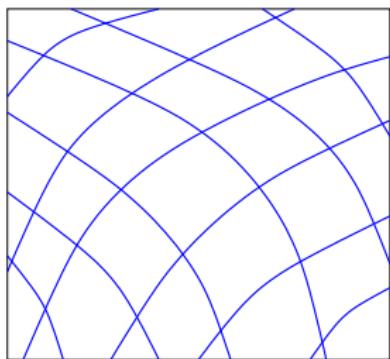
- Rigid: only translation and rotation  $X' = RX + T$
- Affine: parallel lines are transformed into parallel lines  $X' = SRX + T$
- Projective
- Non linear
  - polynomial
  - composition of basis functions (e.g. splines)
  - free-form deformations
  - elastic deformations

$$\mu \nabla^2 u(x, y, z) + (\lambda + \mu) \nabla(\nabla u(x, y, z)) + f(x, y, z) = 0$$

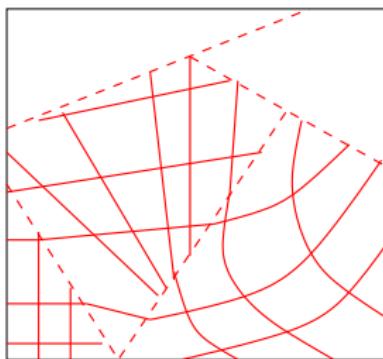
$u(x, y, z)$ : deformation field,  $f$ : external forces,  $\lambda$  and  $\mu$ : elasticity constants

- fluid transformations ( $u$  replaced by velocity field)
- diffeomorphisms

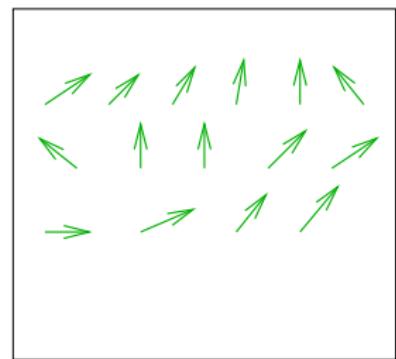
# Gobal / local model



modèle global



modèle par morceaux  
(régional)



modèle local

# Computation of a geometric transform

$$(x', y') = t(x, y)$$

Problems:

- $(x, y) = \text{integer coordinates} \Rightarrow (x', y') ?$
- Calculation?
- Properties?

Example: rotation by  $\pi/4$

$$x' = (x - y) \frac{\sqrt{2}}{2} \quad y' = (x + y) \frac{\sqrt{2}}{2}$$

a	b	c		
d	e	f		
g	h	i		

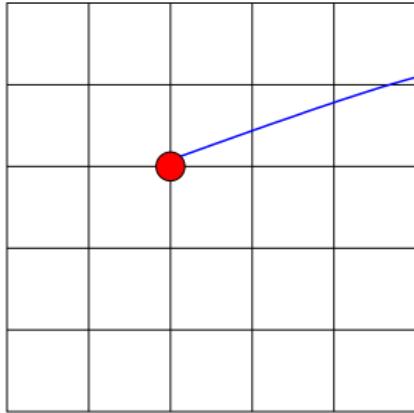
c				
b		f		
ad	e	hi		
g				

Direct transformation

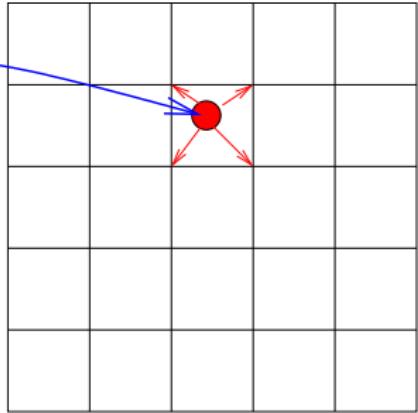
c				
b	e	f		
d	e	h		
g				

Inverse transformation  
(closest point interpolation)

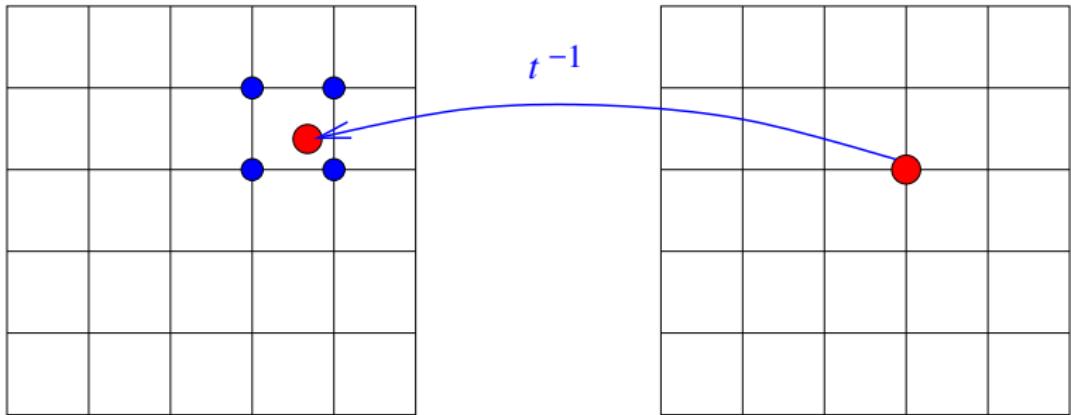
Direct transform:



*t*

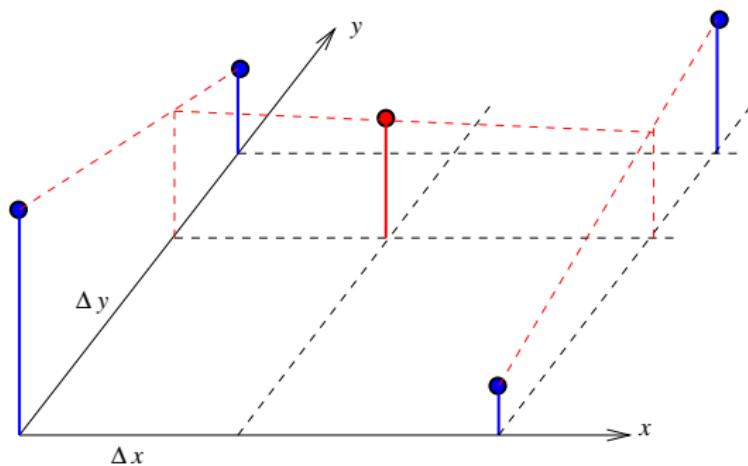


Inverse transform (better when  $t^{-1}$  can be computed):



## Interpolation

- Closest neighbor
  - Linear



$$f(x, y)[(1 - \Delta x)(1 - \Delta y)] + f(x + 1, y)[\Delta x(1 - \Delta y)] + \\ f(x, y + 1)[(1 - \Delta x)\Delta y] + f(x + 1, y + 1)[\Delta x\Delta y]$$

- ### ■ Higher order

# Example

10 rotations by 36 degrees of the original image, with different interpolations:

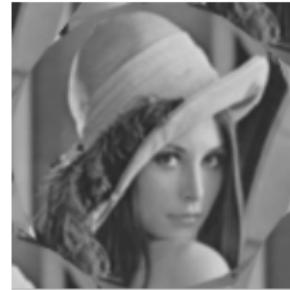
Original



Closest neighbor



Linear



Degree 4 Bspline



Source: <http://bigwww.epfl.ch/demo/jaffine/index.html> (Michael Unser)

# Features

- extrinsic:
  - stereotaxic frame
  - markers
  - calibration of acquisition systems
- intrinsic: related to image content
  - extracted from images:
    - anatomical key points
    - anatomical structures (organs)
    - geometric or differential features (crest lines...)
  - pixel of voxel intensity

Choice: modalities, influence on the distance or similarity criterion

# Similarity and distance (or dissimilarity) criteria

Many!

# Distance between corresponding points

- Hypotheses:

- same number of points  $n$
- known correspondence between  $x_i$  and  $y_i$
- any dimension
- no outliers

- Criterion:

$$E = \sum_{i=1}^n \|x_i - (R(y_i) + T)\|^2$$

- Optimal translation: matching the centers of gravities
- Optimal rotation: closed formula in 2D, quaternion method in 3D, or using SVD.
- Outliers: Replace mean square error by a robust estimator.

# Quaternions

- Definition

$$q = (q_1, q_2, q_3, q_4)^t = (s, v)$$

$s$  = real part

$v$  = imaginary part

- Product:

$$q \times q' = (ss' - v \cdot v', sv' + s'v + v \wedge v')$$

- Conjuguate:  $\bar{q} = (s, -v)$

- Norm:

$$|q|^2 = \bar{q} \times q = q \times \bar{q} = (s^2 + \|v\|^2, 0) = (\|q\|^2, 0)$$

- $\mathcal{Q}_1$  = set of quaternions of norm 1

# Representing rotations by quaternions

- $\mathcal{R}^3$  = set of 3D rotations
- Rotation of axis  $\vec{u}$  and angle  $\theta$ : equivalent to  $(s, v)$  and  $(-s, -v)$  with:

$$s = \cos \frac{\theta}{2}$$

$$v = \sin \frac{\theta}{2} \vec{u}$$

- Equivalence relation:  $\mathcal{R}(q, q') \Leftrightarrow q = -q'$

$\mathcal{R}^3$  isomorphic to  $\mathcal{Q}_1/\mathcal{R}$

$$Rx = q \times x \times \bar{q}$$

## Application to rigid registration

Minimization of  $E = \sum_{i=1}^n \|x_i - R(y_i)\|^2$   
(after applying the best translation)

$$\begin{aligned} E &= \sum_{i=1}^n |x_i - q \times y_i \times \bar{q}|^2 \\ &= \sum_{i=1}^n |x_i - q \times y_i \times \bar{q}|^2 |q|^2 \\ &= \sum_{i=1}^n |x_i \times q - q \times y_i \times \bar{q} \times q|^2 \\ &= \sum_{i=1}^n |x_i \times q - q \times y_i|^2 = \sum_{i=1}^n q^t A_i^t A_i q \end{aligned}$$

Optimal rotation by computing the eigenvalues of

$$A = \sum_{i=1}^n A_i^t A_i.$$

Solution = quaternion which is the eigenvector of norm 1 associated with the smallest eigenvalue of  $A$

# Unknown correspondence

- Reduce complexity:
  - progressive registration starting with the most relevant features
  - constraints (geometry, topology...)
- graph matching
- distance between surfaces

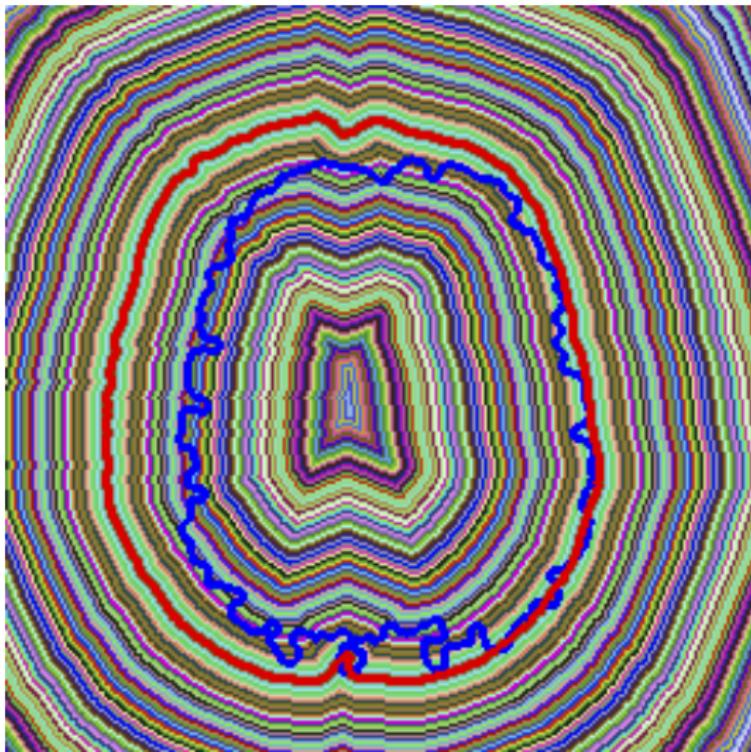
$$d(x, \text{Ref}) = \min_{y \in \text{Ref}} d(x, y)$$

(fast computation, only once)

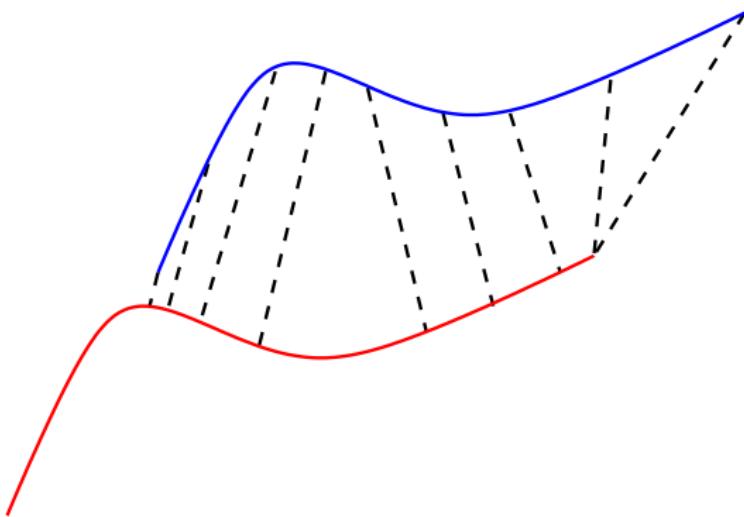
$$d(S, \text{Ref}) = g(d(x, \text{Ref}), x \in S)$$

$g = \min, \max, \text{average}...$

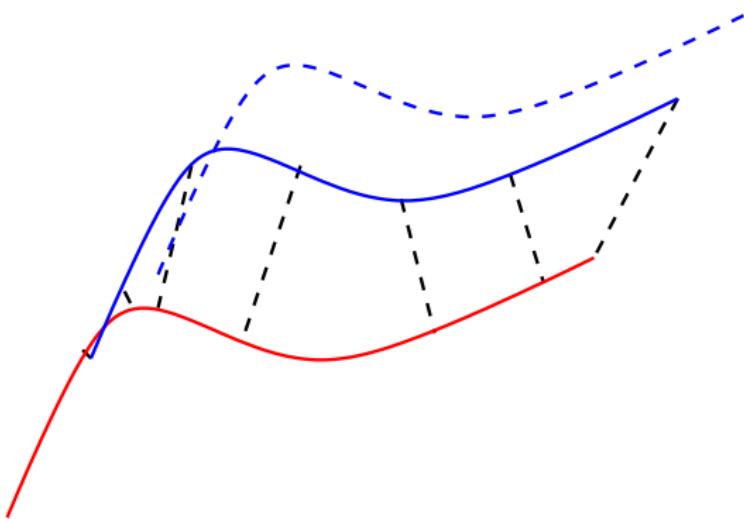
# Distance map



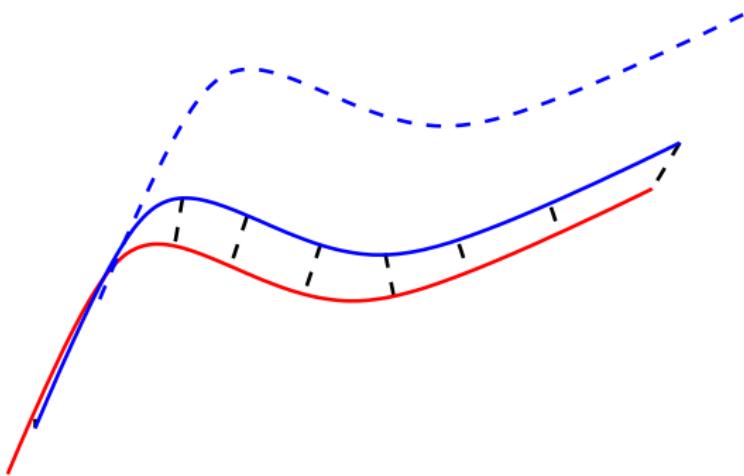
# ICP (Iterative Closest Point)



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# ICP (Iterative Closest Point)



# Intensity based registration: mono-modal case

- Quadratic:

$$E(\Theta) = \sum_x [I_{ref}(x) - I_{rec}(T_\Theta(x))]^2$$

- Quadratic with normalization:

$$E(\Theta) = \sum_x [\frac{\bar{I}_{ref}}{I_{ref}} I_{ref}(x) - I_{rec}(T_\Theta(x))]^2$$

- Correlation:

$$R(\Theta) = \frac{\sum_x [I_{ref}(x) - \bar{I}_{ref}][I_{rec}(T_\Theta(x)) - \bar{I}_{rec}]}{\sqrt{\sum_x [I_{ref}(x) - \bar{I}_{ref}]^2 \sum_x [I_{rec}(T_\Theta(x)) - \bar{I}_{rec}]^2}}$$

(max for the best transformation)

- Robust similarity:  $\rho = M\text{-estimateur}$

$$E(\Theta) = \sum_x \rho[I_{ref}(x) - I_{rec}(T_\Theta(x))]$$

# Examples of robust estimators

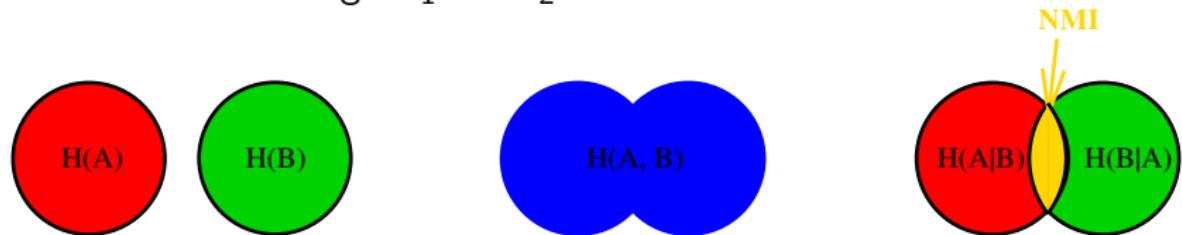
- quadratic
- truncated quadratic
- attenuated quadratic (Geman - McLure)
- quadratic for small errors, then linear (Huber)

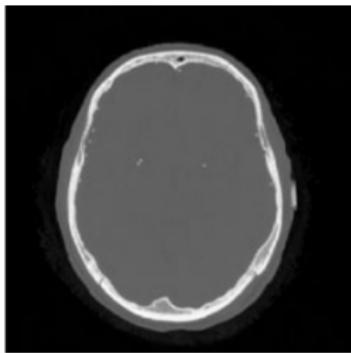
# Intensity based registration: multi-modal case

Use of the joint histogram: maximization of mutual information

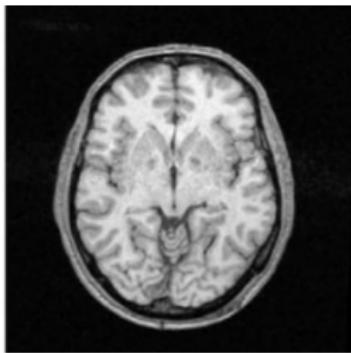
$$E(\Theta) = - \sum_g \sum_k p(g, k) \log \frac{p(g, k)}{p(g)p(k)}$$

$g, k$ : intensities in images  $I_1$  and  $I_2$

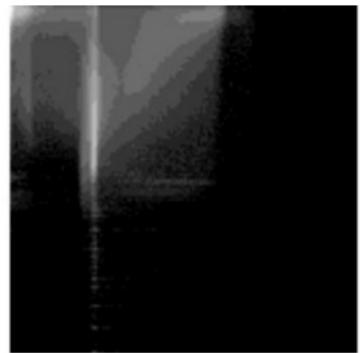




(a)



(b)



(c)

Fig. 1. Example of a feature space for (a) a CT image and (b) an MR image. (c) Along the axes of the feature space, the gray values of the two images are plotted: from left to right for CT and from top to bottom for MR. The feature space is constructed by counting the number of times a combination of gray values occurs. For each pair of corresponding points  $(\mathbf{x}, \mathbf{y})$ , with  $\mathbf{x}$  a point in the CT image and  $\mathbf{y}$  a point in the MR image, the entry  $(I_{CT}(\mathbf{x}), I_{MR}(\mathbf{y}))$  in the feature space on the right is increased. A distinguishable cluster in the feature space is the stretched vertical cluster, which is the rather homogeneous area of brain in the CT image corresponding to a range of gray values for the MR image.

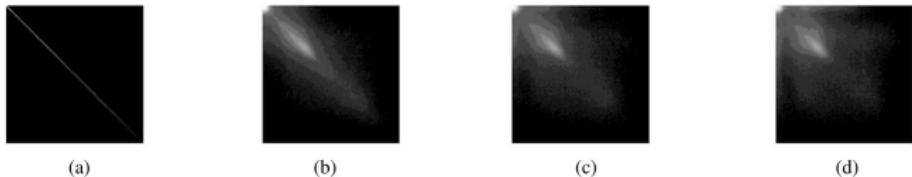


Fig. 2. Joint gray value histograms of an MR image with itself. (a) Histogram shows the situation when the images are registered. Because the images are identical, all gray value correspondences lie on the diagonal. (b), (c), and (d) show the resulting histograms when one MR image is rotated with respect to the other by angles of  $2^\circ$ ,  $5^\circ$ , and  $10^\circ$ , respectively. The corresponding joint entropy values are (a) 3.82; (b) 6.79; (c) 6.98; and (d) 7.15..

Figures from [Pluim et al. 2003]

# Optimization

- Typical algorithms: gradient, conjugated gradient, Powell, simplex, Levenberg-Marquardt, Newton-Raphson, geometric hashing...
- Local minima  $\Rightarrow$  importance of initialization
- Stochastic optimization, genetic algorithms, simulated annealing...
- Multi-scale
- Specific methods in some cases (e.g. ICP)

# Interactivity?

- **Automatic:** not always desirable
- **Interactive:** difficult in 3D, lacks reproducibility
- **Semi-automatic:** defining the right level of interaction (initialization, control, corrections...)

# Validation and evaluation

Ground truth?

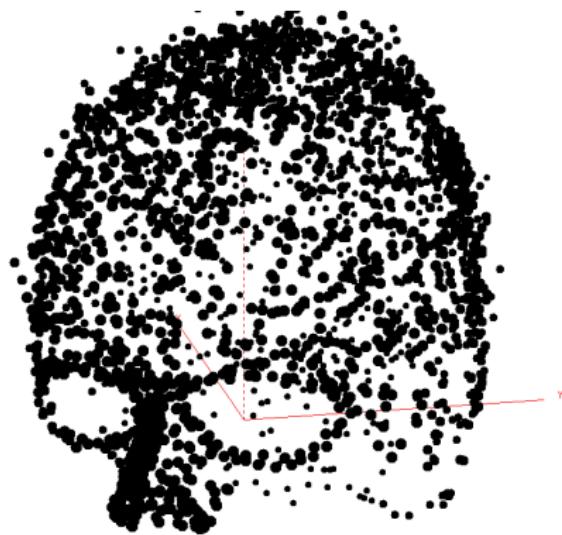
## Criteria:

- intrinsic precision of the algorithm
- precision, robustness
- reliability
- resources required
- algorithmic complexity
- practical use

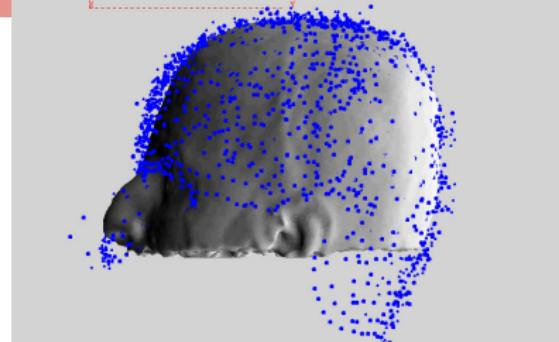
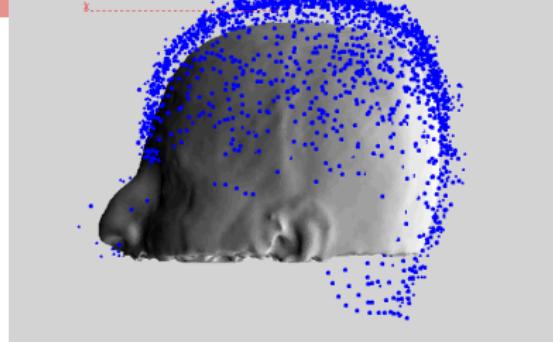
## Different levels of test:

- simulations
- phantoms
- real data

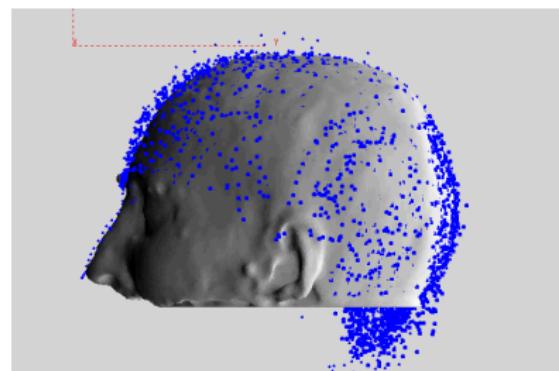
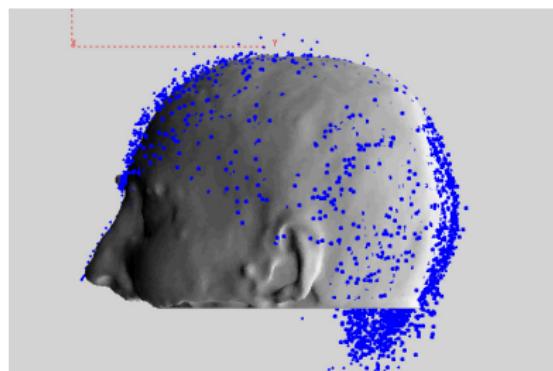
# MRI + headshape in EEG/MEG (Jérémie Pescatore)



## MRI + headshape in EEG/MEG ( Jérémie Pescatore)

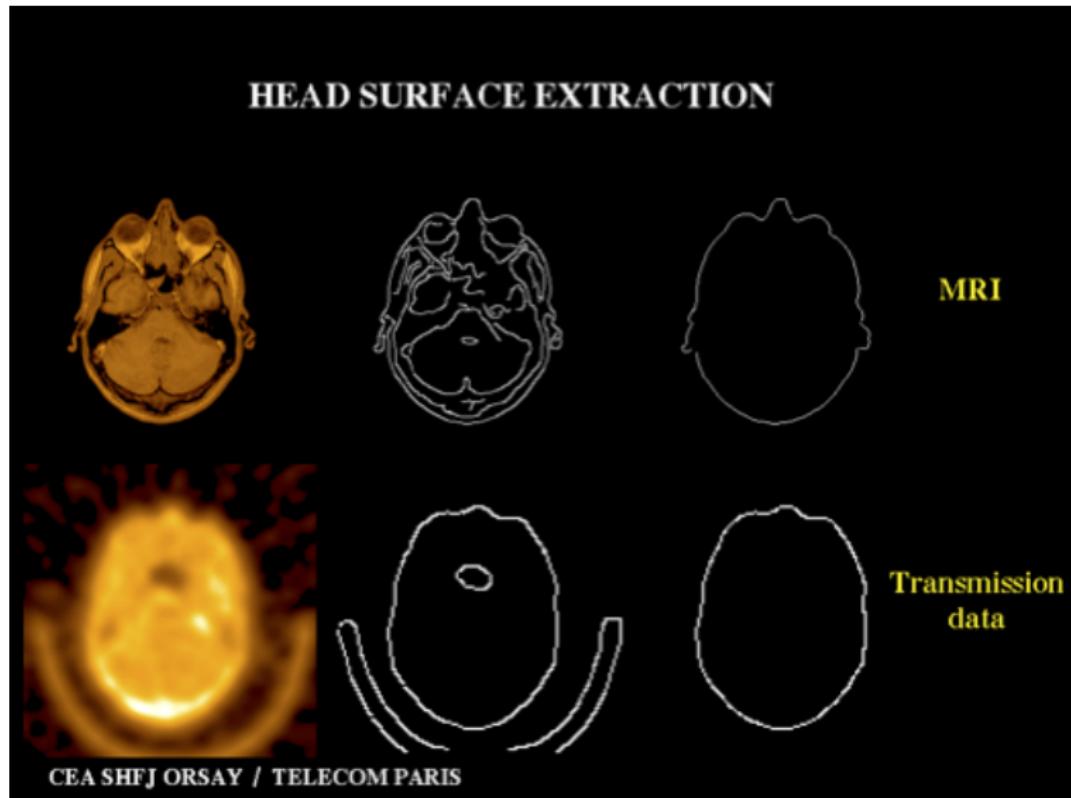


fonction de proximité=2.1 mm



fonction de proximité=1.80 mm

# Rigid registration of brain images (Jean-François Mangin)



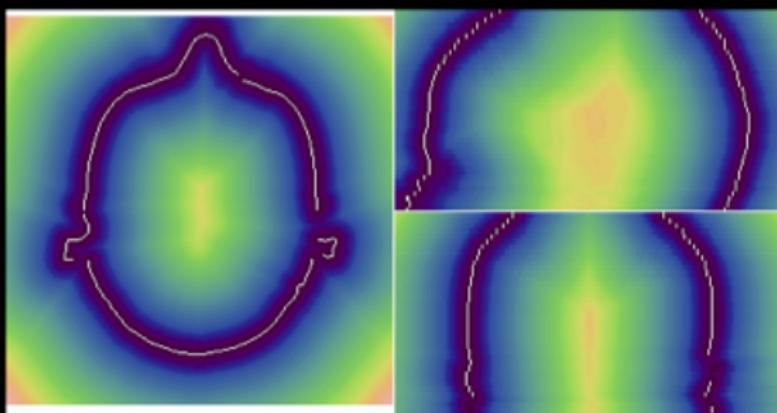
# Rigid registration of brain images (Jean-François Mangin)

## 3D DISTANCE MAP TO THE MRI HEAD SURFACE

AXIAL

SAGITTAL

CORONAL



CEA SHFJ ORSAY / TELECOM PARIS

# Rigid registration of brain images (Jean-François Mangin)

## SURFACE MATCHING

GENERALIZED DISTANCE

MINIMIZATION:

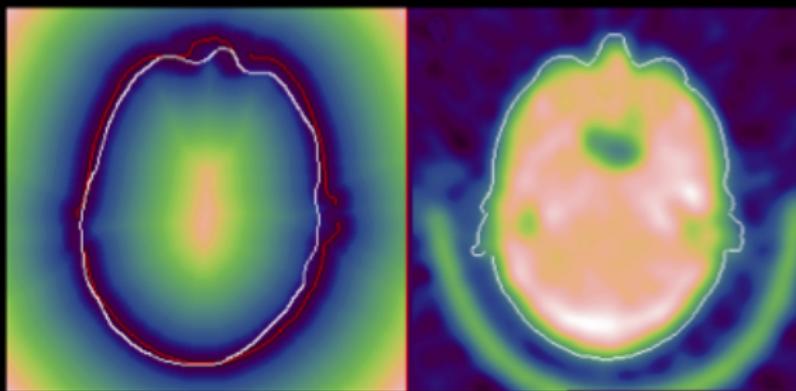
A POSITION OF THE  
MOBILE SURFACE IN  
THE 3D DISTANCE MAP

RESULT :

PET TRANSMISSION

+

MRI HEAD SURFACE

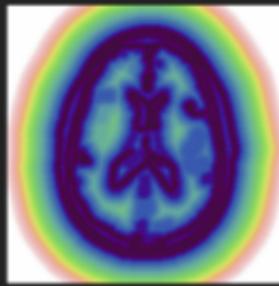
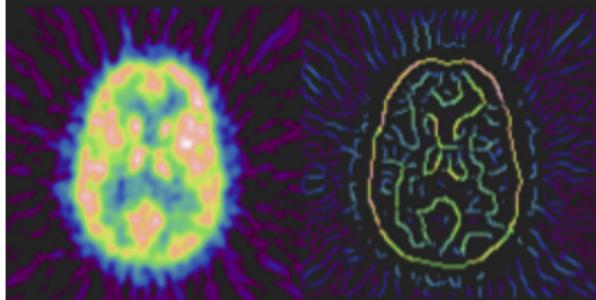


CEA SHFJ ORSAY / TELECOM PARIS

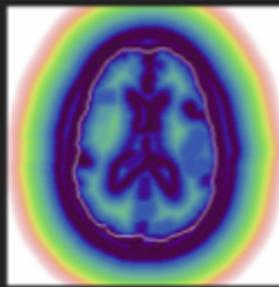
# Rigid registration of brain images (Jean-François Mangin)

## SECOND REGISTRATION

Extraction of the brain surface (PET)



Precomputation  
of a  
3D distance map  
to the  
MRI edges

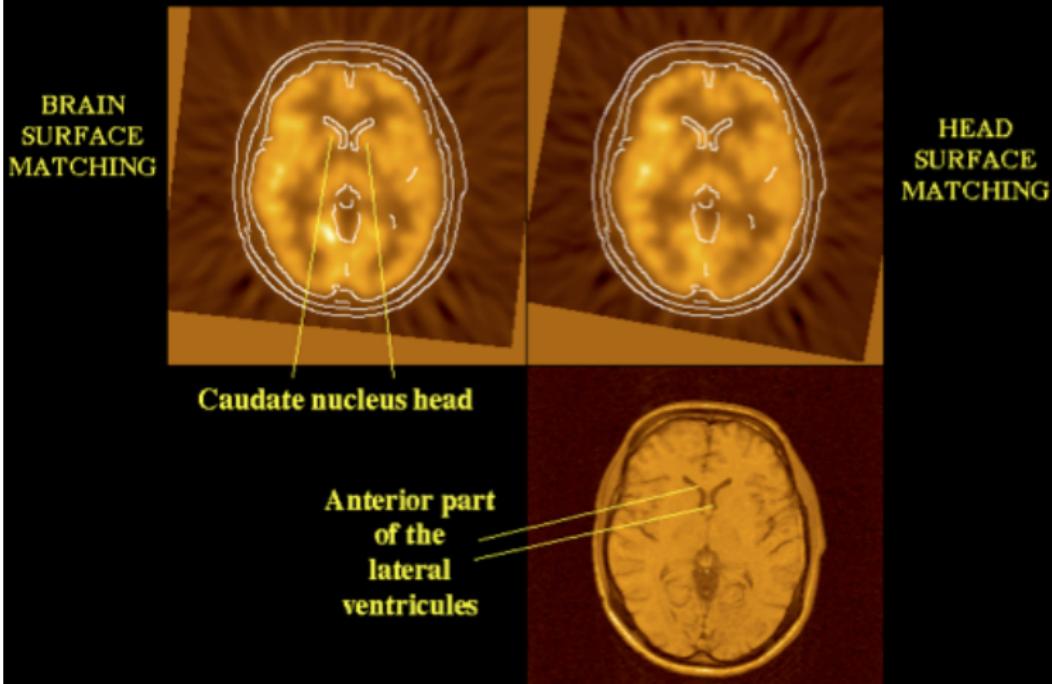


Brain surface  
matching

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# Rigid registration of brain images (Jean-François Mangin)

## MOTION BETWEEN PET TRANSMISSION AND EMISSION ACQUISITIONS



# Rigid registration of brain images (Jean-François Mangin)

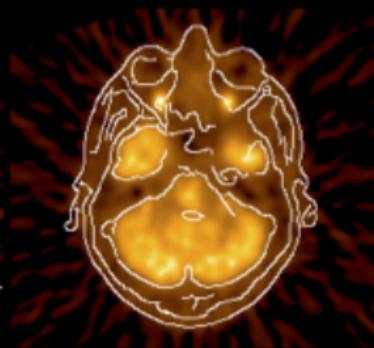
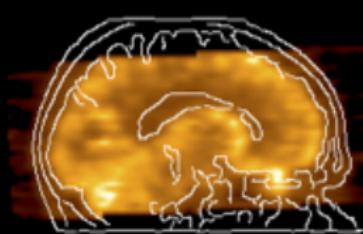
## MRI / PET 3D REGISTRATION : FDG

PET + MRI EDGES

SAGITTAL

AXIAL

CORONAL

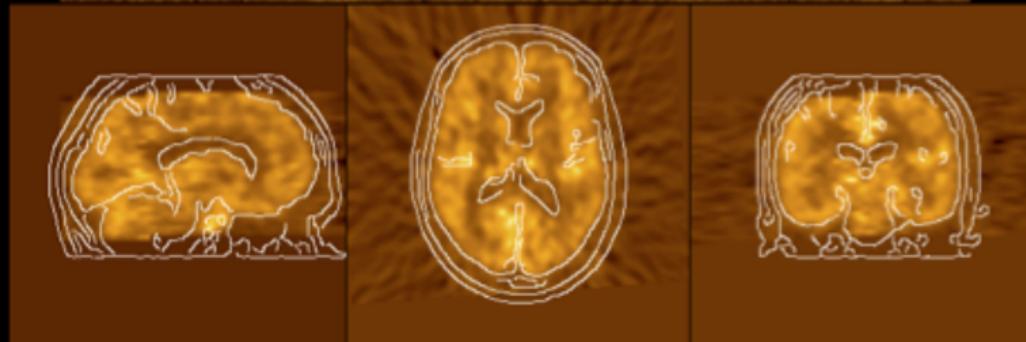
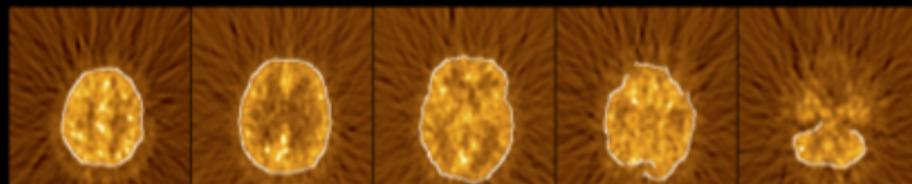


CEA SHFJ ORSAY / TELECOM PARIS

# Rigid registration of brain images (Jean-François Mangin)

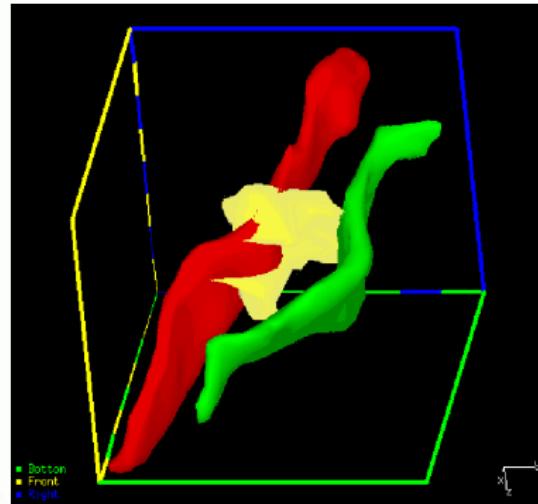
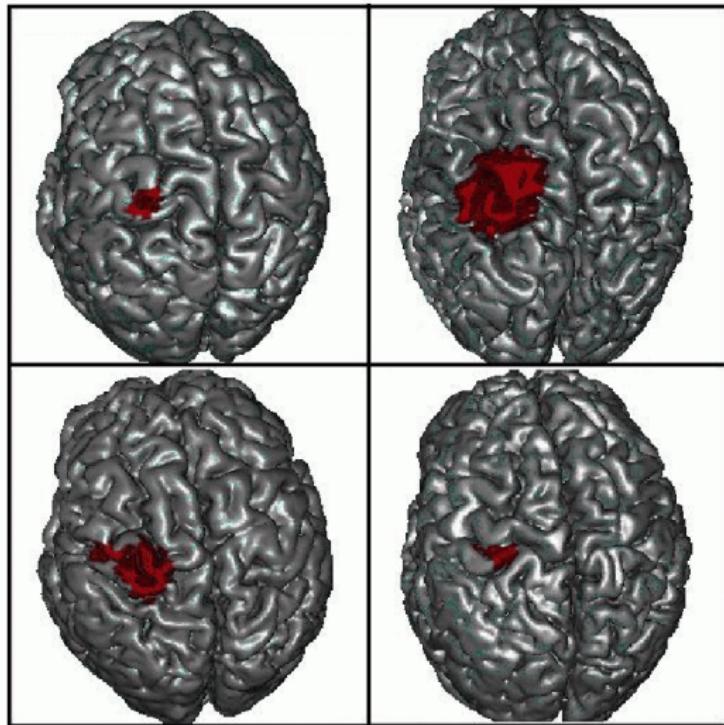
MRI / PET 3D REGISTRATION :  $\text{H}_2\text{O}^{15}$

PET + PET BRAIN SURFACE : A FEW SLICES



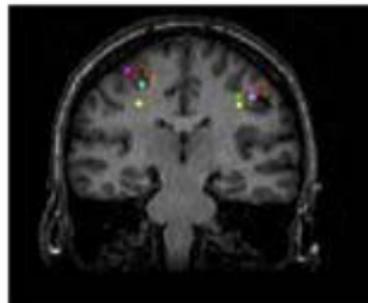
PET + MRI EDGES : SAGITTAL, AXIAL AND CORONAL SLICES

# Anatomo-functional registration

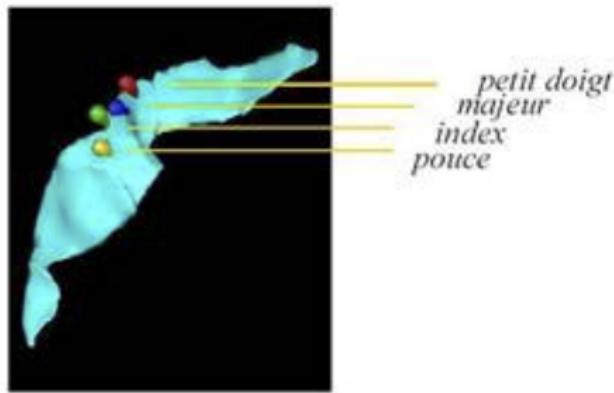
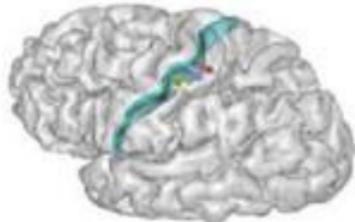


# Anatomo-functional registration

## SOMESTHESIE : Somatotopie des doigts



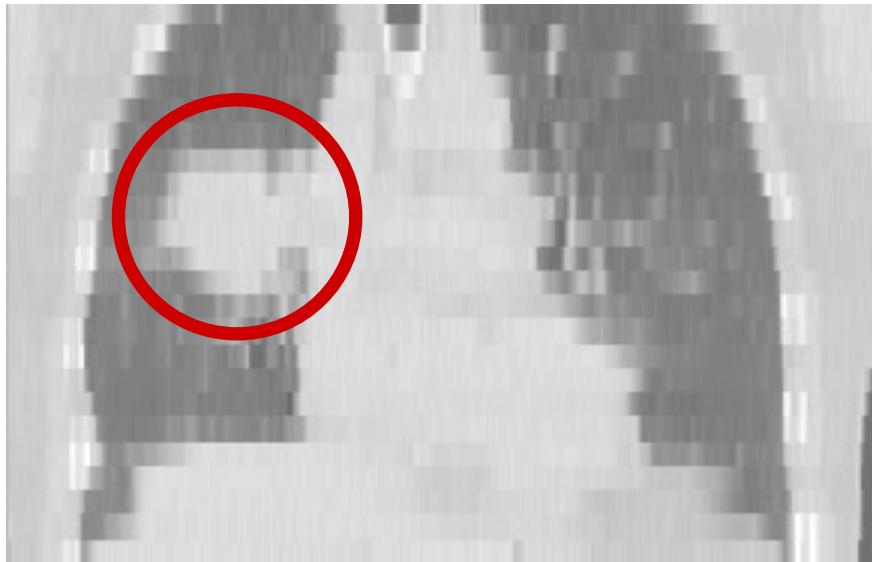
Distance entre doigt ~ 0.9 cm  
Distance I - V ~ 1.5 cm



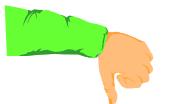
# Non linear registration: chest images (Oscar Camara)

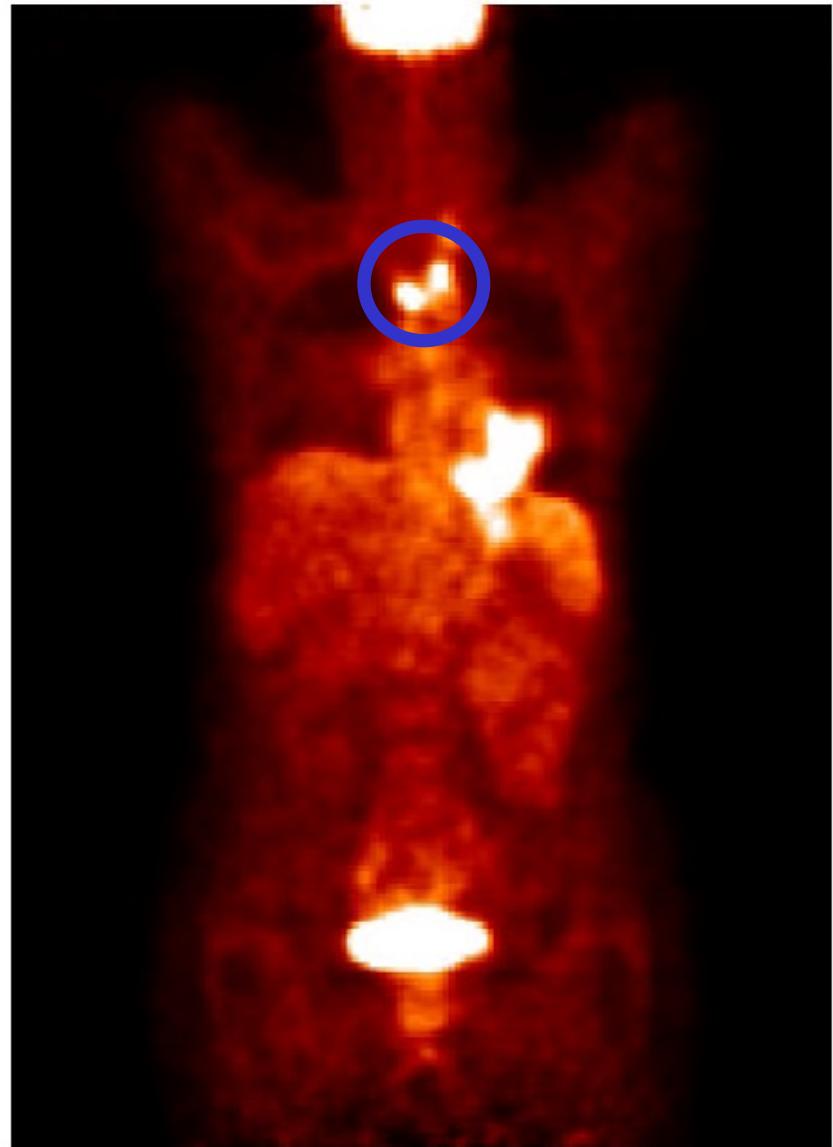
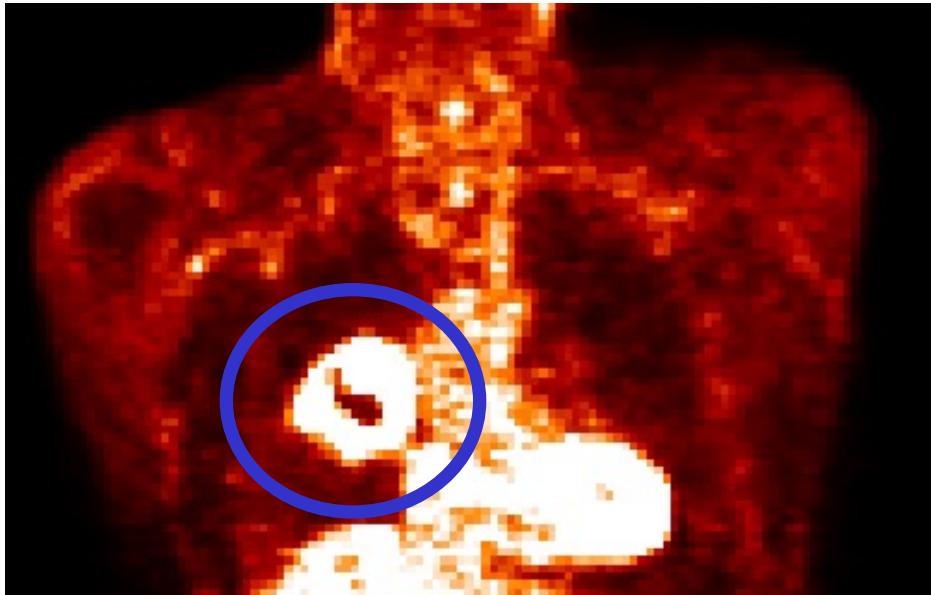
# Introduction: CT images

- Anatomical information 
- Accurate localization and morphology of organs 
- No lesion malignancy information 
- Sometimes tumours not distinguishable

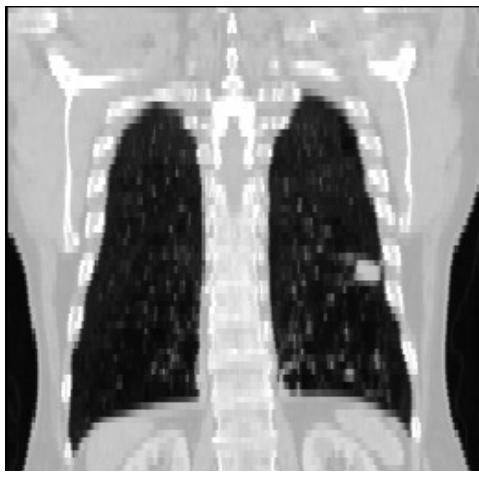


# Introduction: PET images

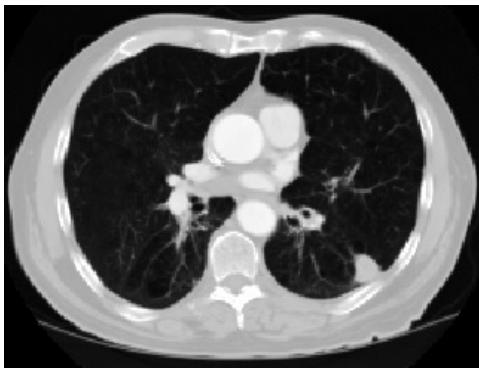
- Metabolic information, staging 
- High sensitivity and specificity 
- Poor image quality 
- Little anatomical information 



# Introduction: PET-CT application

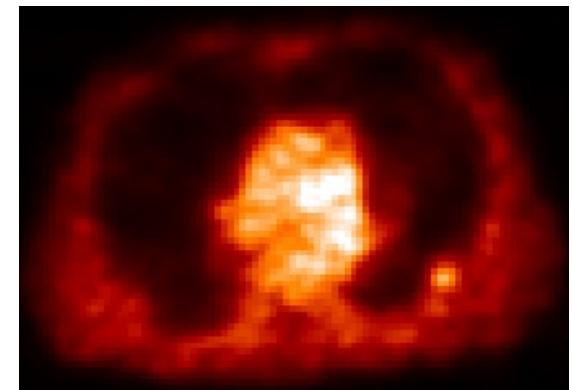
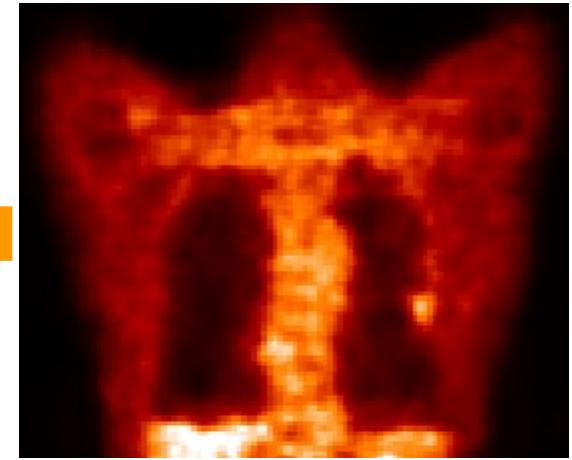


Anatomy  
(localization)



CT

Functionality  
(detection)



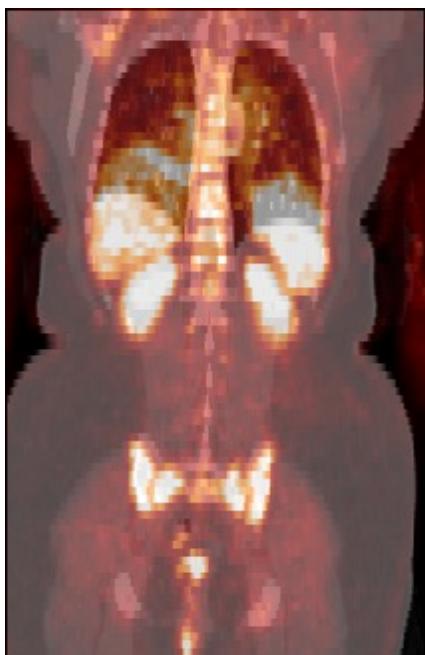
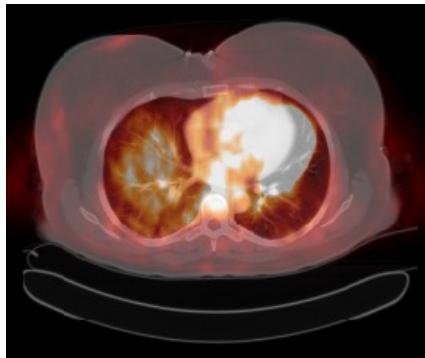
PET



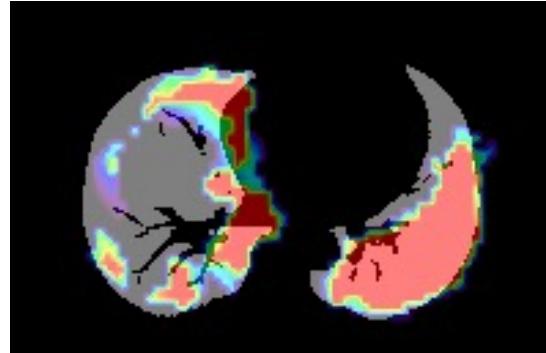
CT + PET

# Registration context: linear registration

*Grey level*

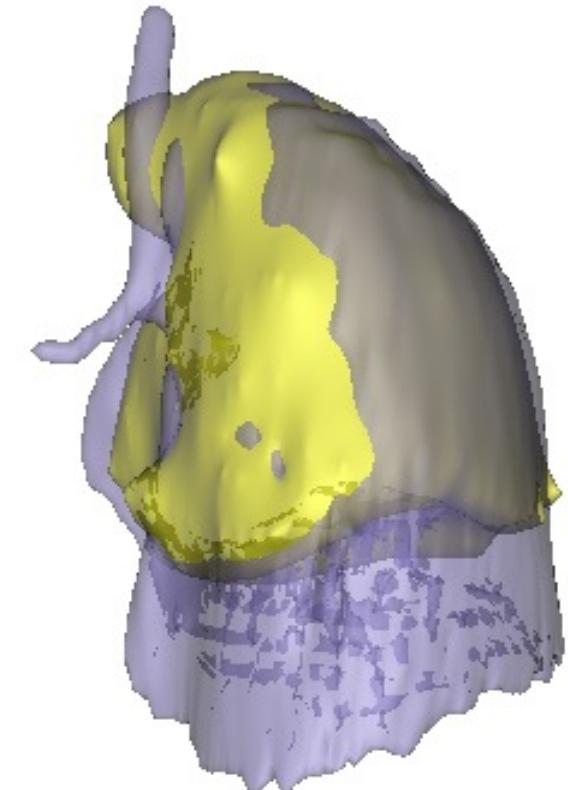


*Segmented lungs, 2D*



- *CT lungs*
- *PET lungs*

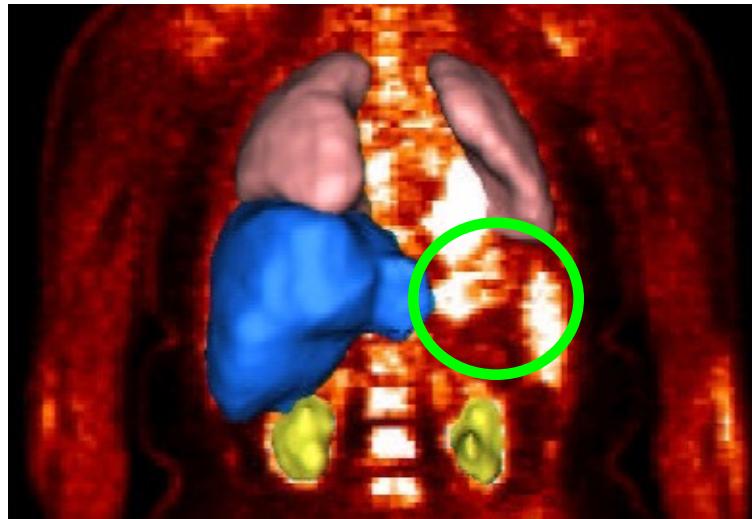
*Segmented lungs, 3D*



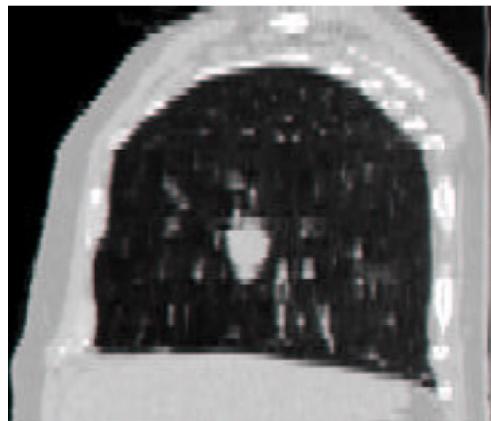
- *CT lungs*
- *PET lungs*

# Registration context: structure-based methods

No information far from the landmarks

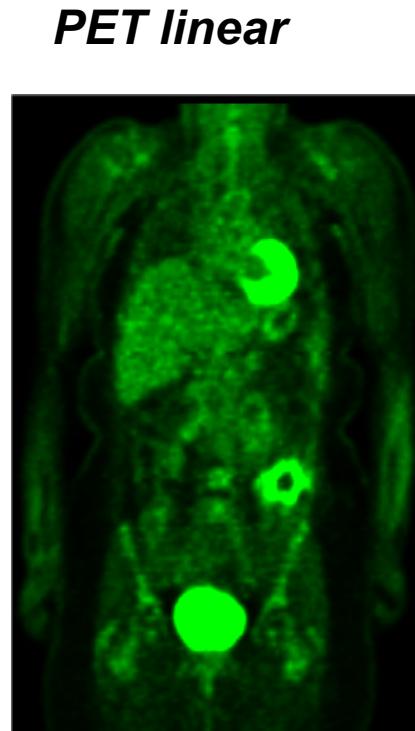
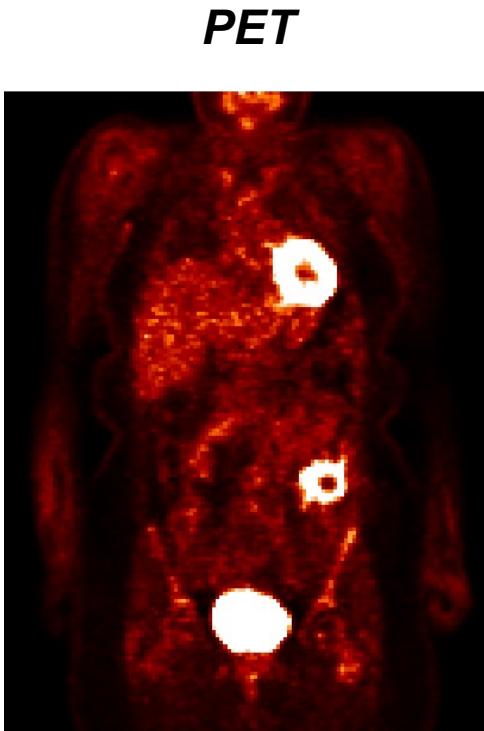
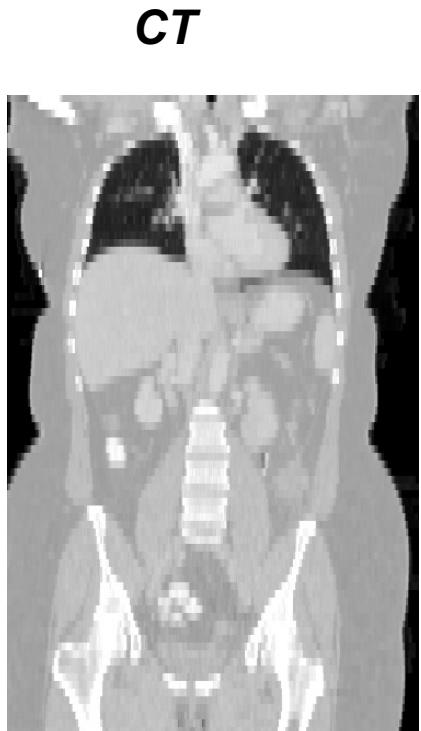


Loss of information “within” the structure



# Registration context: Free-Form Deformations

- FFD with a previous affine registration phase



# Proposed methodology

## Structure-based

- accuracy limited by segmentation
- no information far from segmented structures

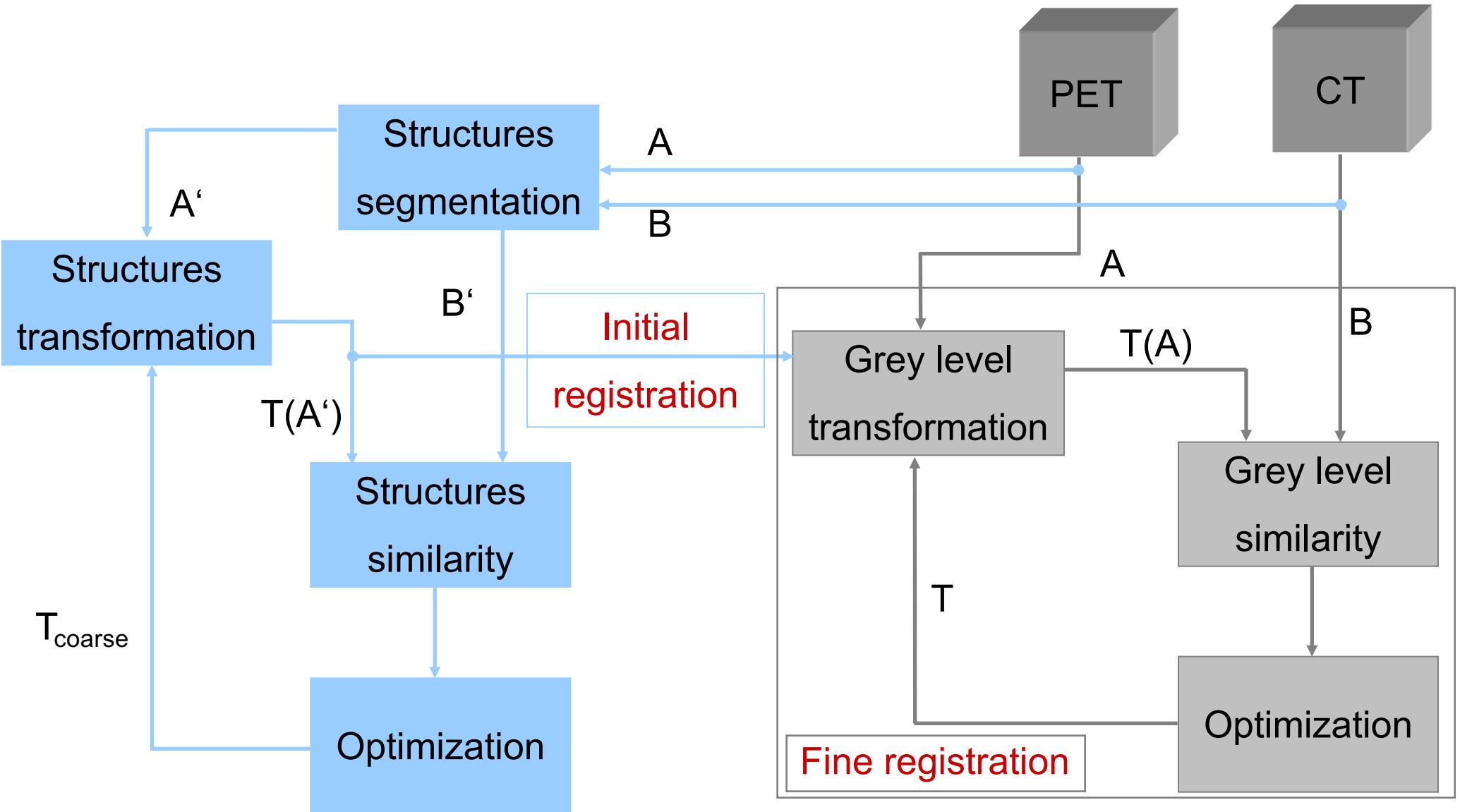
## Grey level-based methods

- difficulty of working with PET images
- computational cost

## Original solution:

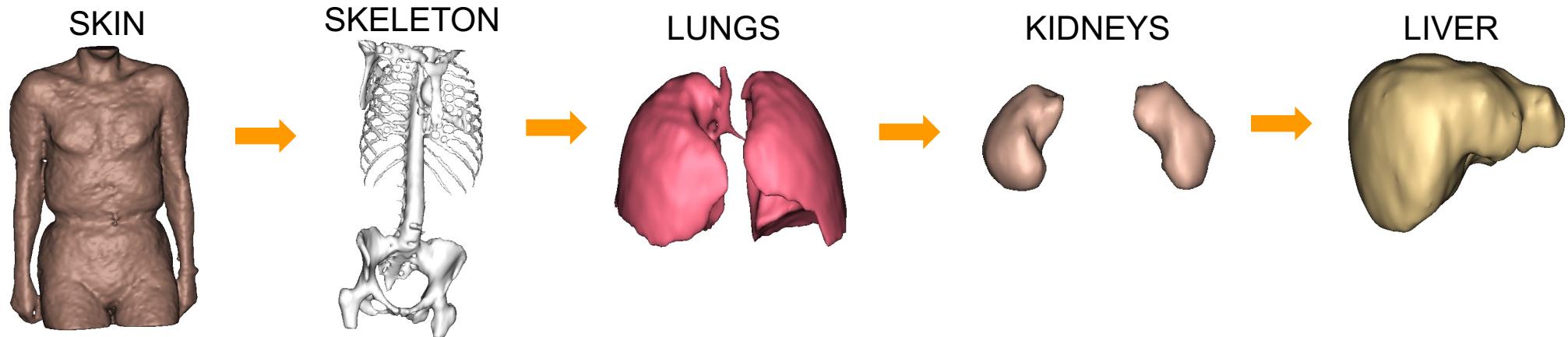
- combine both strategies
- anatomical 2-level scheme
- use of anatomical information to constrain the search of global solution

# Proposed methodology

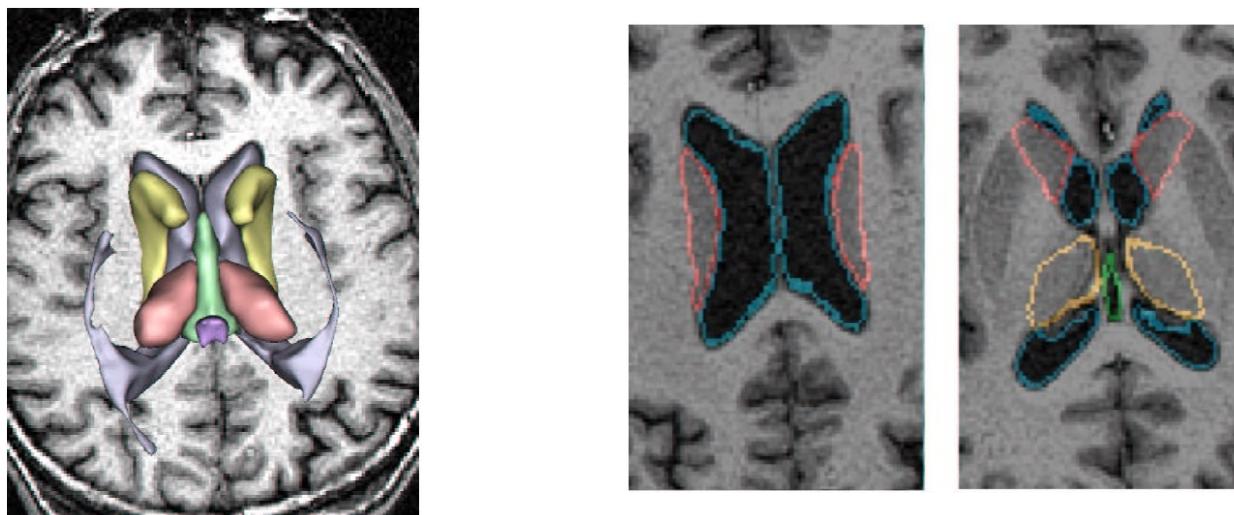


# Initial registration: structure segmentation

- Choice and order of structures to segment



- Similar strategy used in a brain internal structure segmentation application [Colliot-Camara, SPIE'04]

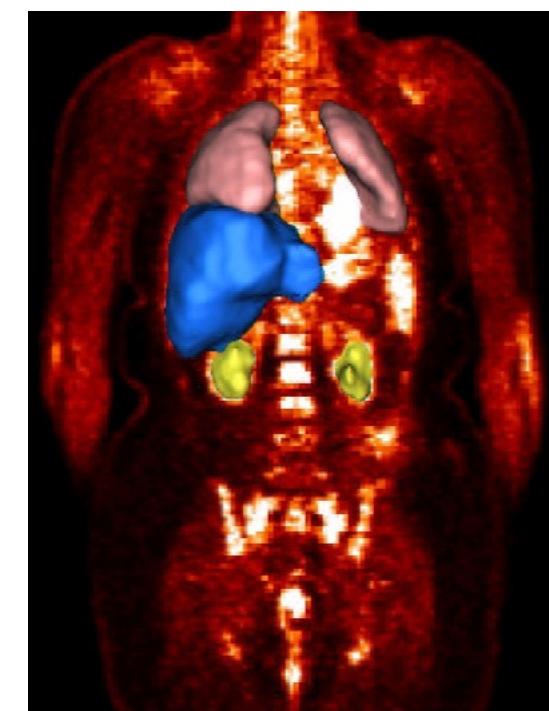
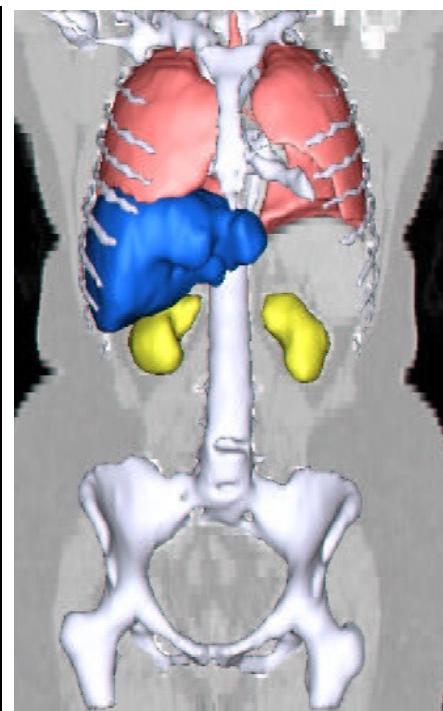


# Initial registration: structure segmentation

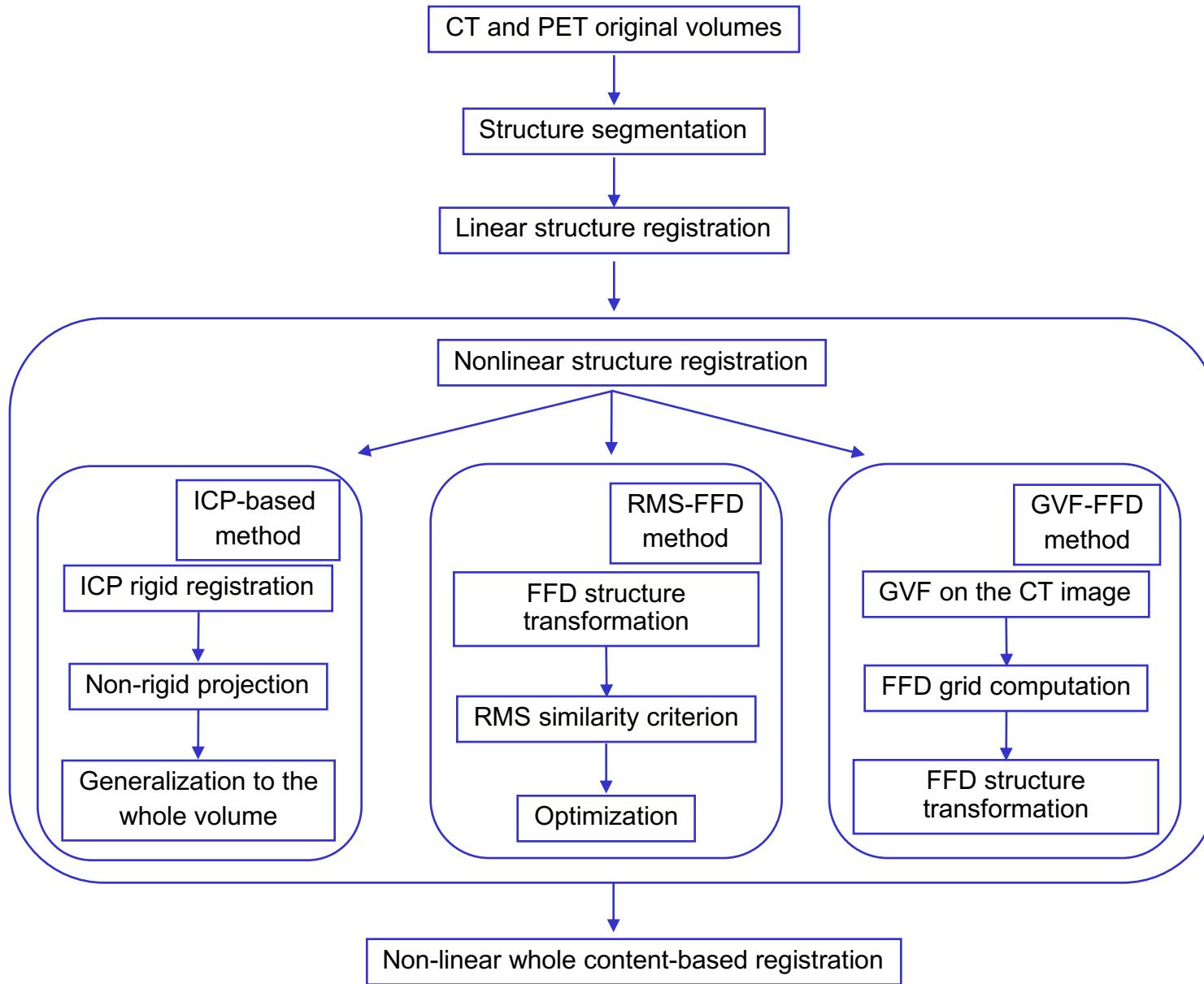
*2D segmentation results*



*3D segmentation results*

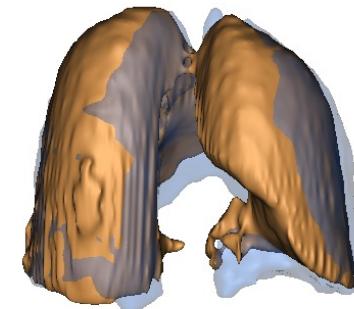
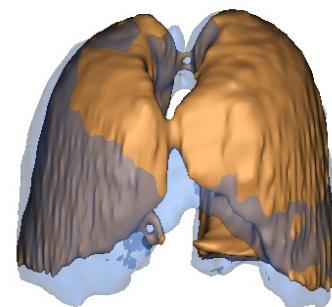
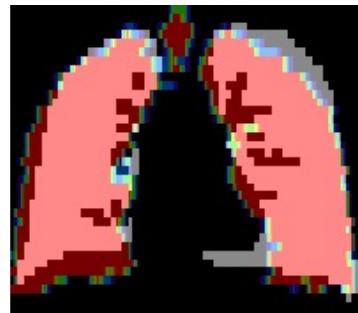


# Initial registration: structure registration

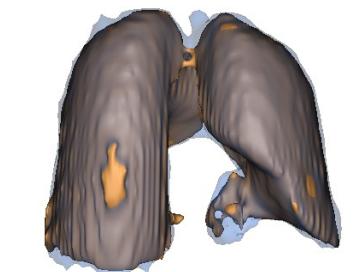
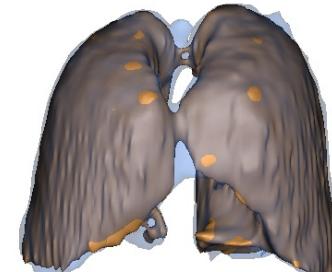


# Initial registration: structure registration, RMS-FFD

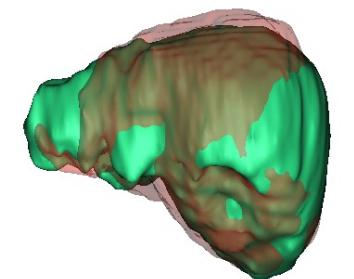
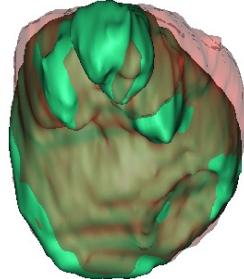
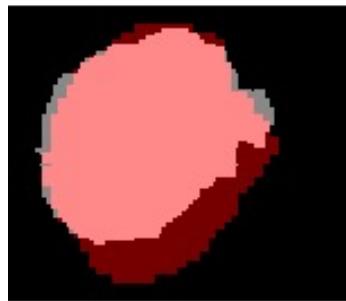
*Linear*



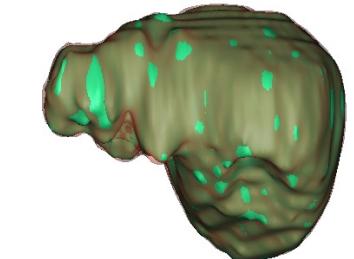
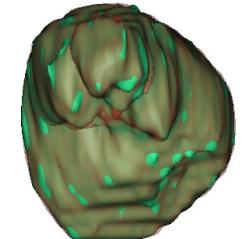
*RMS-FFD*



*Linear*

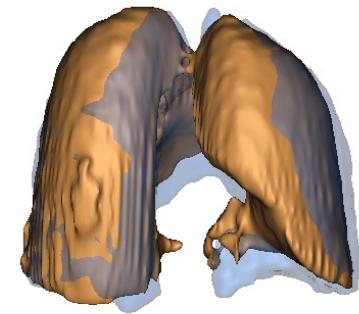
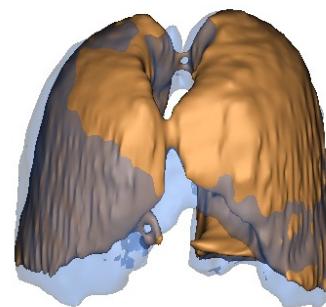
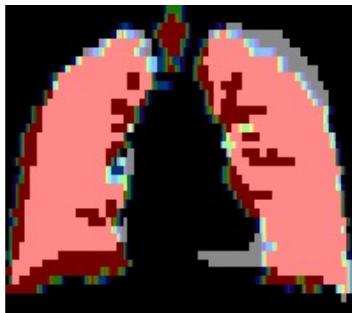


*RMS-FFD*

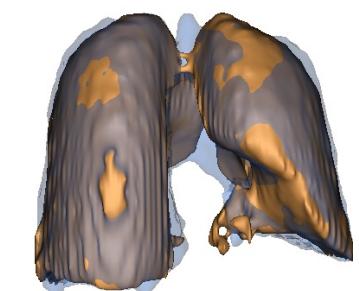
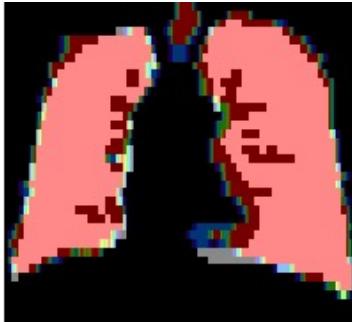
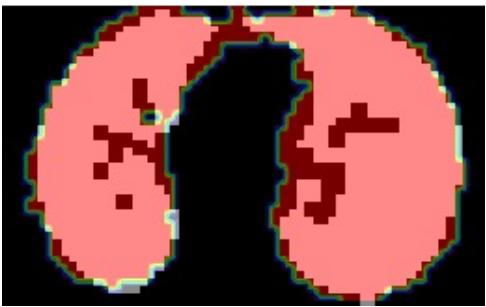


# Initial registration: structure registration, GVF-FFD

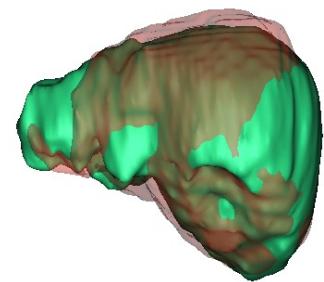
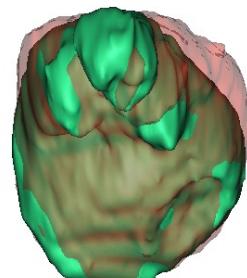
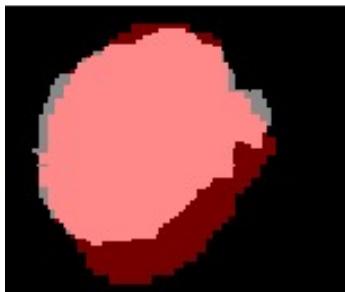
*Linear*



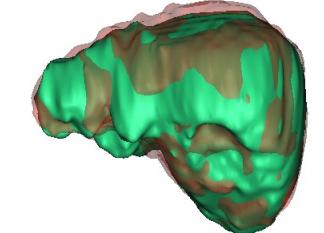
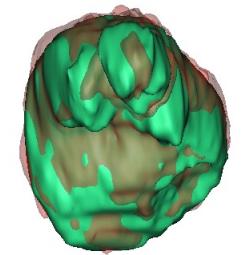
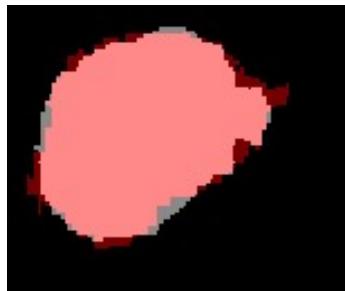
*RMS-FFD*



*Linear*



*RMS-FFD*



# Initial registration: structure registration

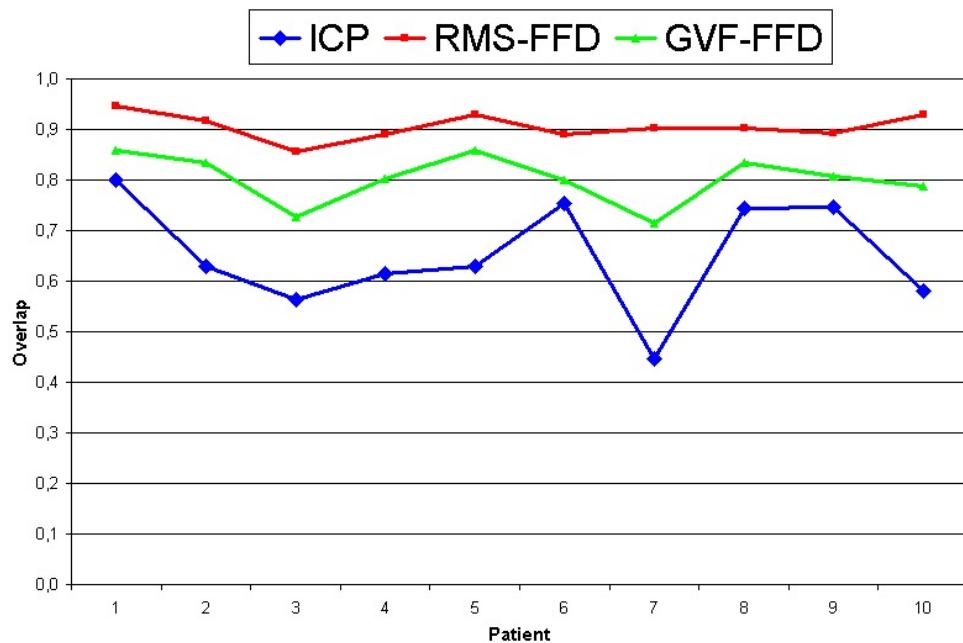
- Evaluation of the structure registration phase
  - comparison between ICP-based, RMS-FFD and GVF-FFD
  - two quantitative measures:
    - Overlap Measure (OM) applied on segmented structures

$$OM = \frac{|A \cap B|}{|A \cup B|}$$

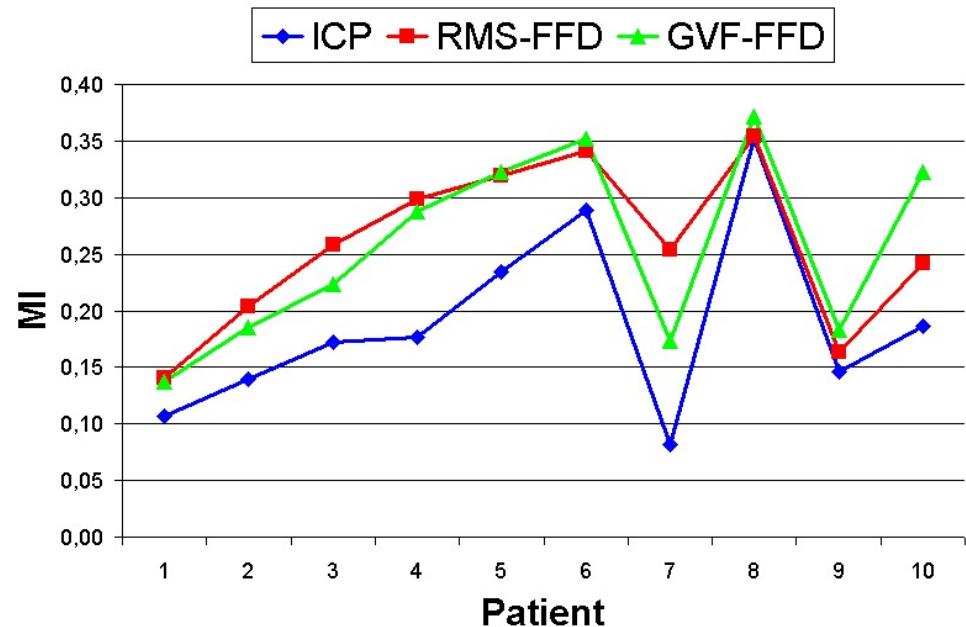
- Mutual Information (MI) between:
  - grey-level CT
  - grey-level PET, registered by applying the transformation computed over the surfaces

# Initial registration: structure registration

STRUCTURES OVERLAP



MUTUAL INFORMATION



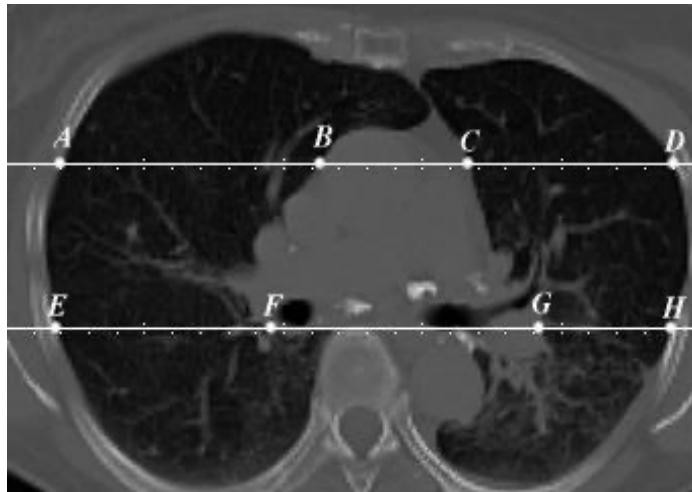
Method	ICP	RMS-FFD	GVF-FFD
Overlap(value/%)	0.6586/100	0.9030/137.095	0.8275/122.081
MI(value/%)	0.1888/100	0.2592/137.286	0.2486/131.697
Time (μs/pixel)	6.60723	699.365	52.610

# Fine registration: similarity measure

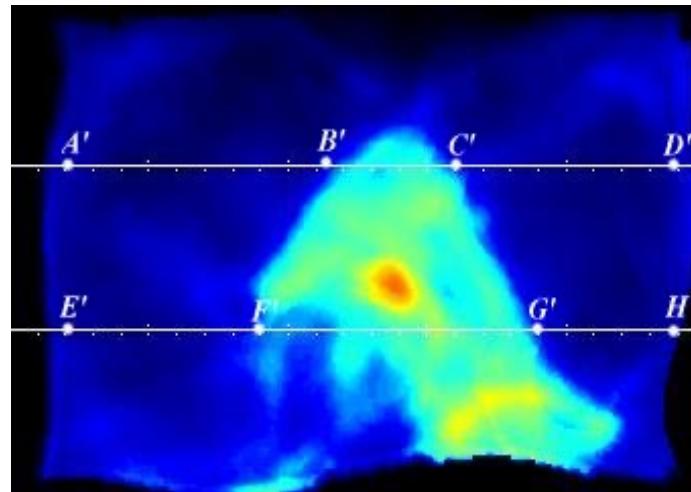
- Problem
  - in multimodal applications, non-functional relation among image grey-level values
- Solution
  - Mutual Information, MI [Viola95, Collignon95], and its variant, Normalized Mutual Information, NMI [Studholme99]

# Evaluation of the algorithm

- Original fast evaluation protocol designed with medical experts:
  - several anatomically significant slices are presented, marked with a ruler that defines some reference points



A/A'=Anterior Left Chest Wall  
C/C'=Anterior Right Mediastinal Wall  
E/E'=Posterior Left Chest Wall  
G/G'=Posterior Right Mediastinal Wall



B/B'=Anterior Left Mediastinal Wall  
D/D'=Anterior Right Chest Wall  
F/F'=Posterior Left Mediastinal Wall  
H/H'=Posterior Right Chest Wall

# Evaluation of the algorithm

- Registration in each reference point is classified according to a scoring scale

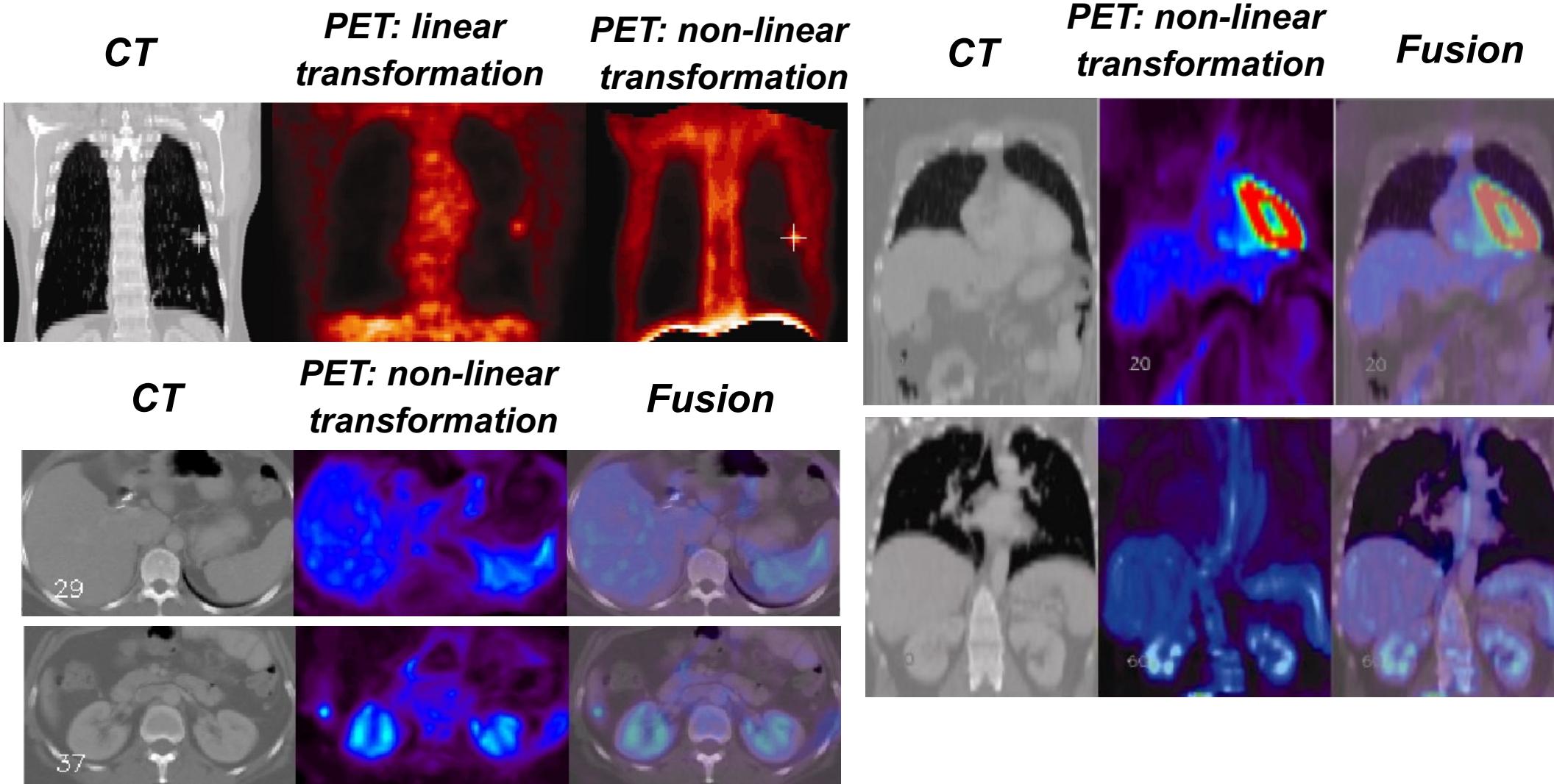


Scale	mm	quality
0	0-5	Good
1	5-15	Acceptable
2	15-	Unacceptable

- Inter-observer consistency is good enough (3 evaluators)

Region	Mean	Variance
Lungs	0.670	0.02
Kidneys	0.172	0.01
Liver	0.720	0.11
Heart	0.935	0.09
Stomach	1.833	0.08

# Results

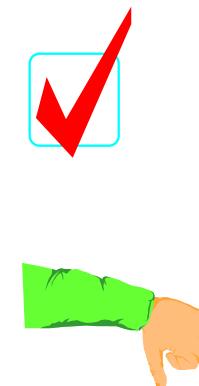
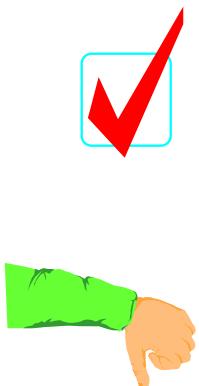


# Results

- 3 independent evaluators from 3 different hospitals
- Evaluation of 5 different thoracic and abdominal cases
- Statistics on the scoring scale

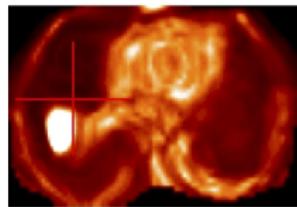
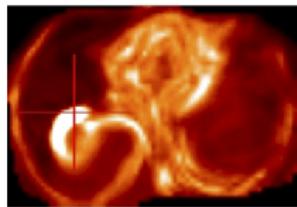
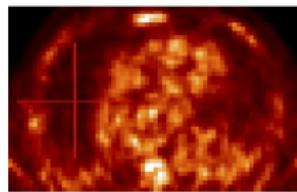
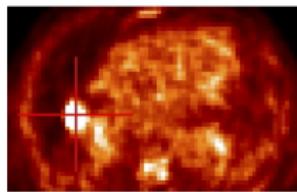
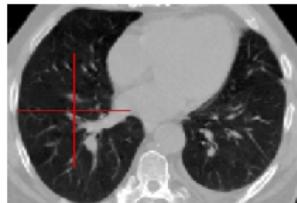
***Inter-patient results***

Region	Mean	Variance	Max	Min
Lungs	0.615	0.01	0.64	0.60
Kidneys	0.120	0.01	0.21	0.05
Liver	0.467	0.15	0.87	0.16
Heart	0.597	0.15	1.44	0.54
Stomach	1.833	0.11	2.00	1.33



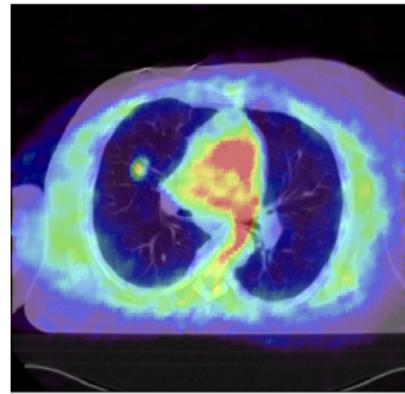
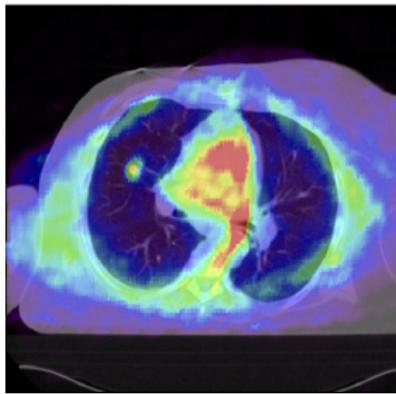
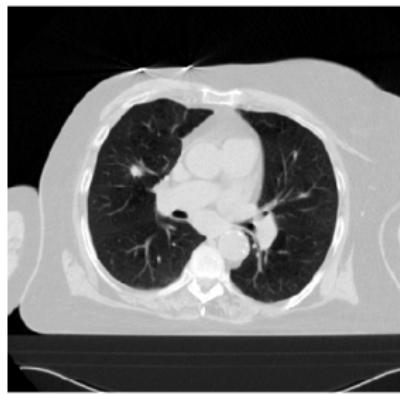
# Pathological cases (Antonio Moreno)

Without constraints:



# Pathological cases (Antonio Moreno)

With constraints on the tumor:

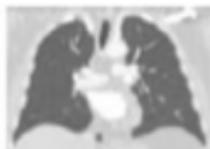


# Using a breathing model (A. Moreno, S. Chambon)

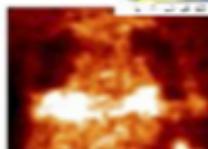
- Image data



CT at end-expiration

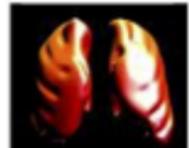
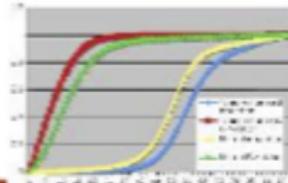


CT at end-inspiration

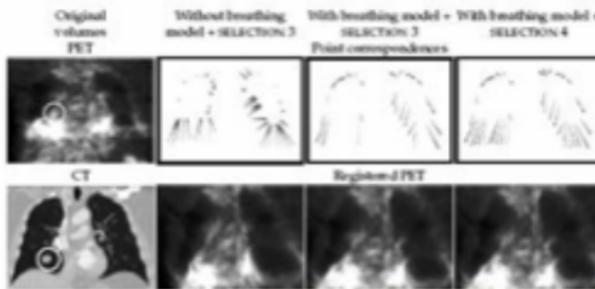


PET

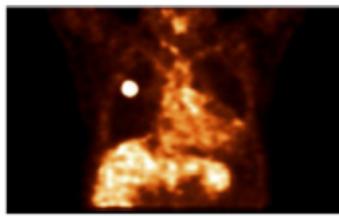
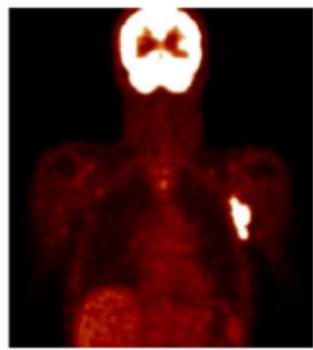
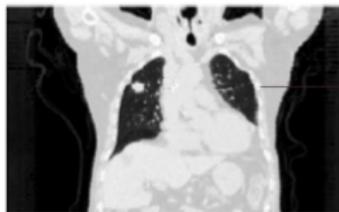
- Breathing model



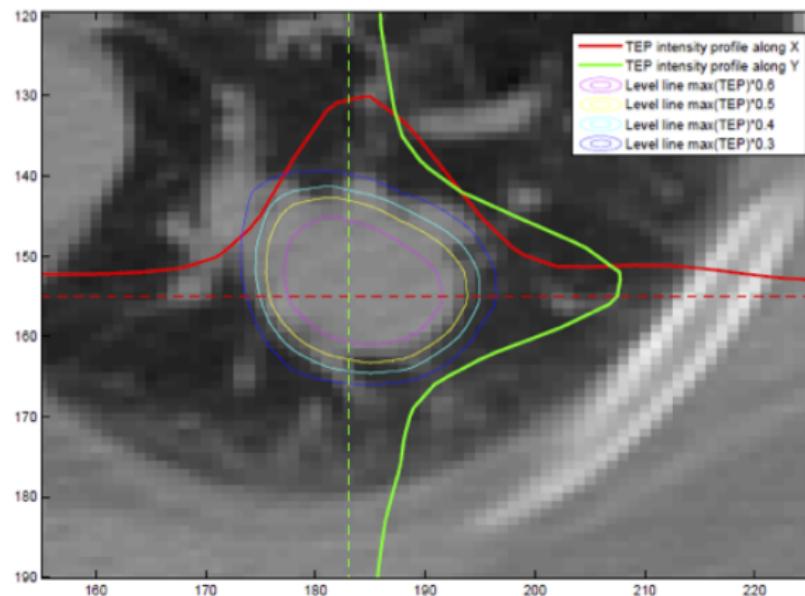
- Optimal model-based registration of PET & CT lung images



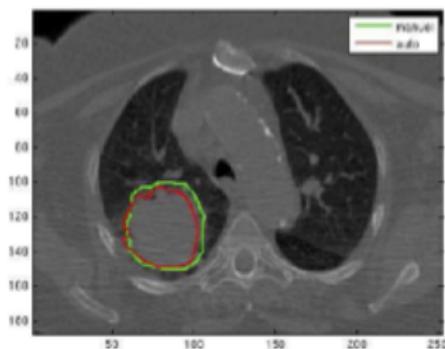
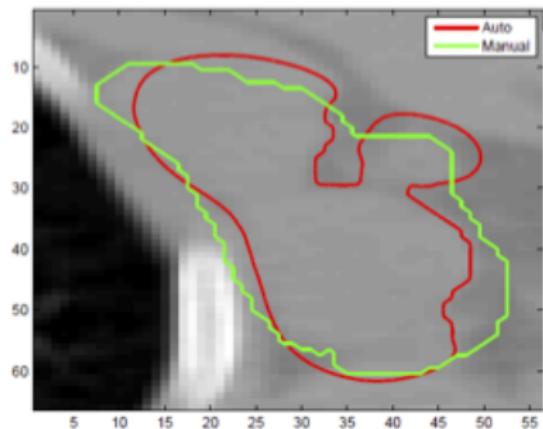
# PET-CT fusion (tJulien Wojak)



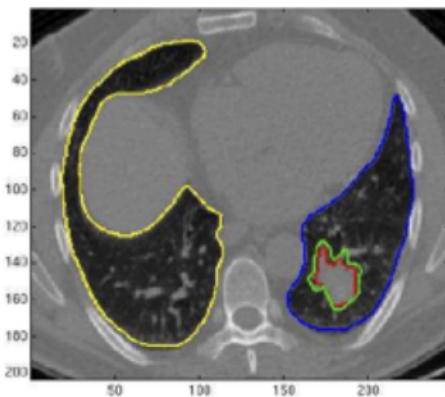
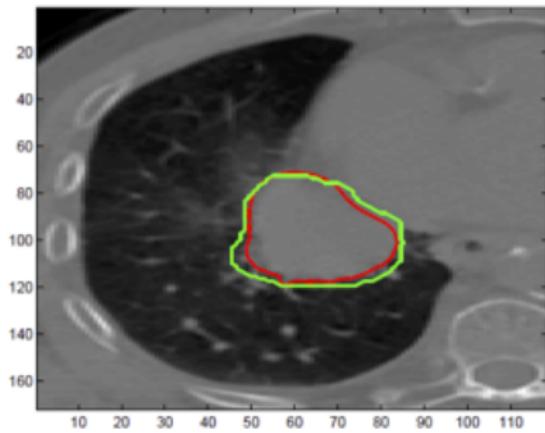
# PET-CT fusion (tJulien Wojak)



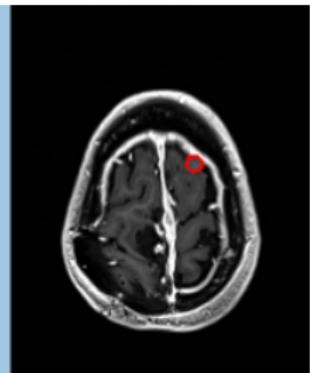
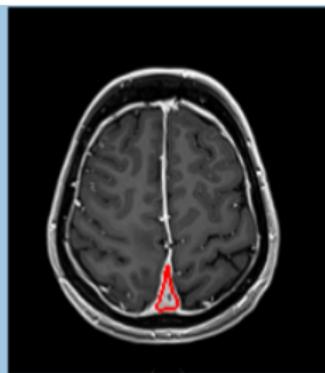
# PET-CT fusion (tJulien Wojak)



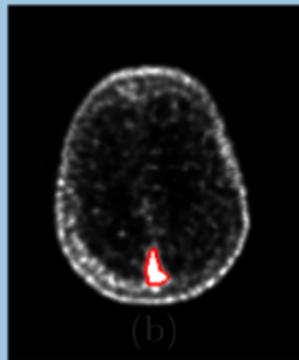
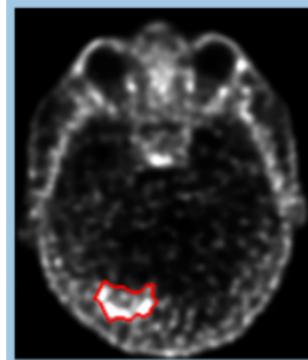
# PET-CT fusion (tJulien Wojak)



# PET-MRI fusion (Hélène Urien)



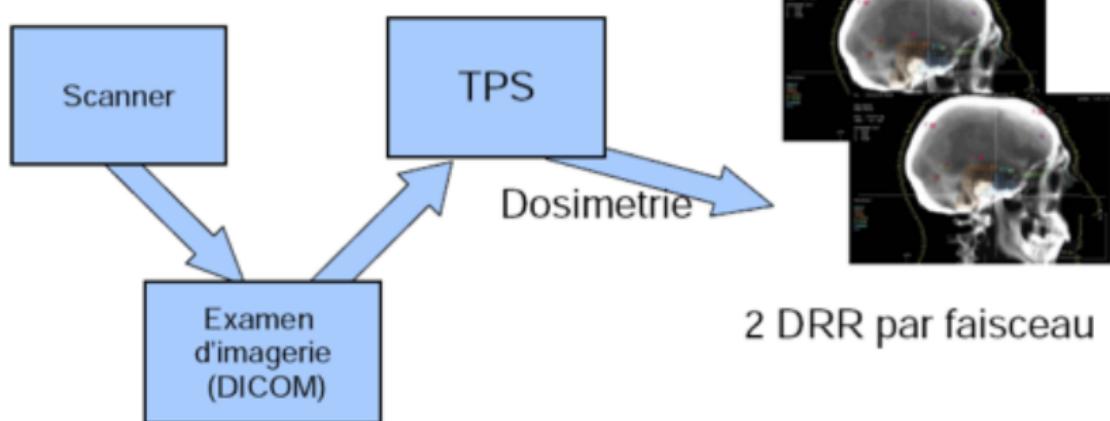
(a)



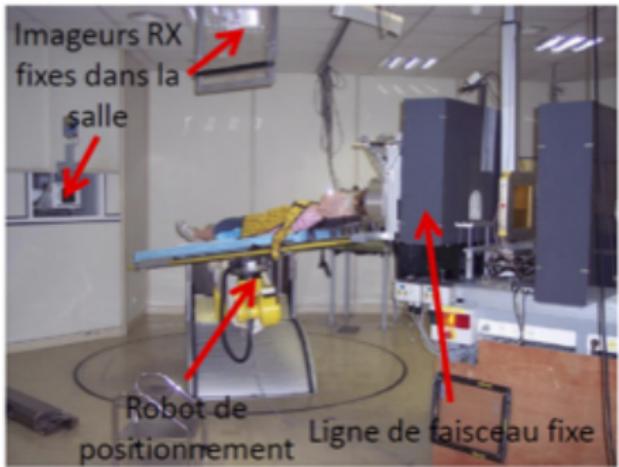
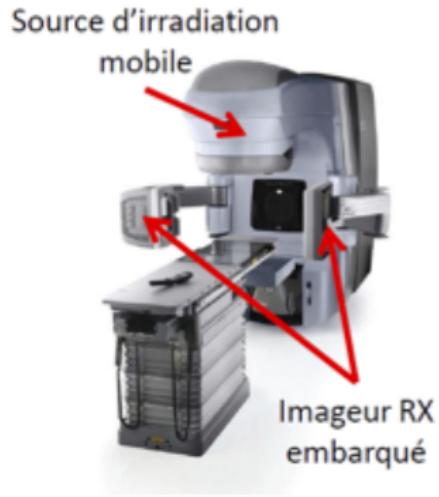
(b)

# Protontherapy

Avant traitement (hors salle)

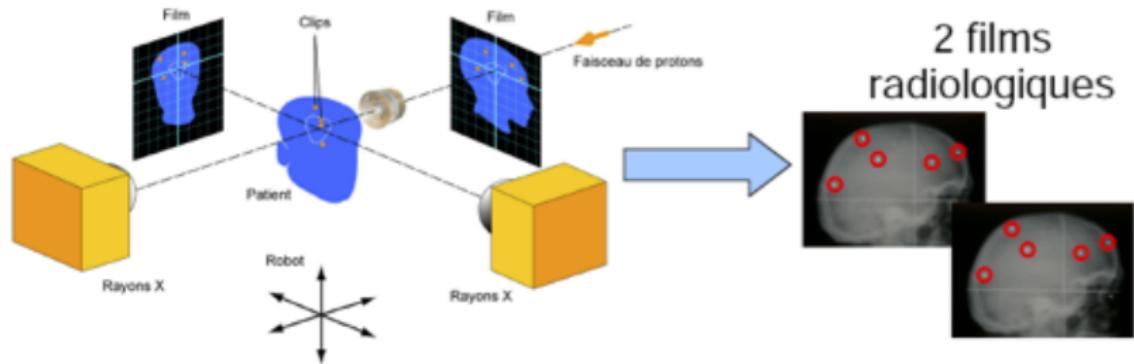


# Protontherapy



# Protontherapy

Etapes avant traitement (dans la salle de traitement)



Confrontation et recalage films / DRR

# Examples of registration software tools

- ITK: <http://www.itk.org/>
- Brain Visa: <http://brainvisa.info/>
- FSL: <http://www.fmrib.ox.ac.uk/fsl/>
- Mipav: [https://mipav.cit.nih.gov/pubwiki/index.php/Optimized\\_automatic\\_registration\\_3D](https://mipav.cit.nih.gov/pubwiki/index.php/Optimized_automatic_registration_3D)
- 3D Slicer:  
<https://www.slicer.org/wiki/Slicer3:Registration>
- ...

## A few references

- J. Modersitzki (2004). Numerical methods for image registration. Oxford university press.
- J. V. Hajnal, D. L.G. Hill, D. J. Hawkes (2001). Medical image registration. CRC press.
- J. P. W. Pluim (2003). Mutual information based registration of medical images: a survey. IEEE Transactions on Medical Imaging.